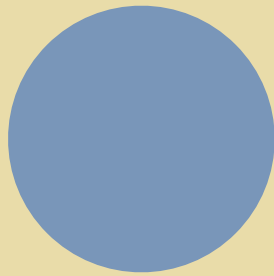
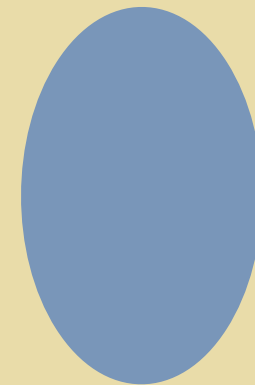


Polarized Black Holes in AdS



Lauren Greenspan



[hep-th/1511.08505 Costa, LG, Oliveira, Penedones, Santos]

Motivation

- Find interesting new geometries in AdS.
- Study Black Hole Polarization
- What can we learn about the dual field theories?

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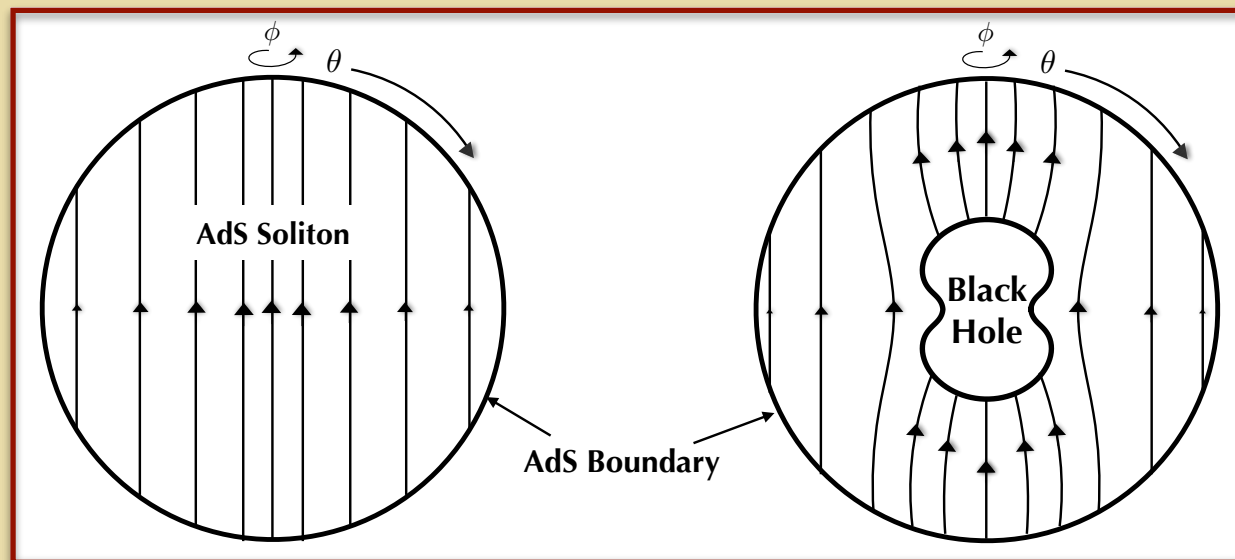
Idea

- Study the thermodynamics of deformed 4-dimensional black holes subject to a dipolar potential $A_\tau = i\mathcal{E} \cos \theta$ that are dual to a 3-dimensional field theory.

Gravity Set-up

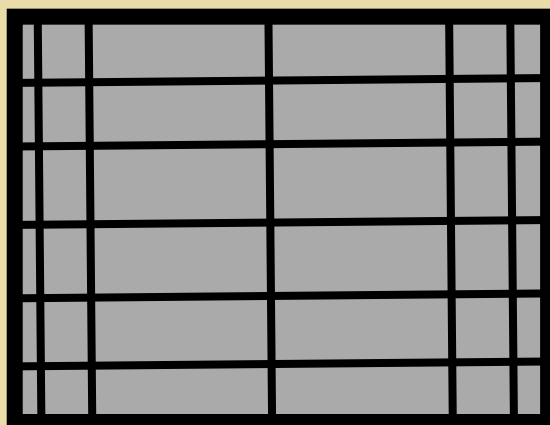
$$S = \frac{1}{16\pi G_N} \int d^4x \sqrt{-g} \left(R + \frac{6}{l^2} - F_{\alpha\beta} F^{\alpha\beta} \right) + \frac{1}{8\pi G_N} \int d^3x \sqrt{h} K$$

- gauge field \tilde{A}_μ
- metric $g_{\mu\nu}$



Study numerical solutions
Einstein-Maxwell gravity
with a dipolar potential
source.

$$R_{\mu\nu} + \frac{3}{l^2} g_{\mu\nu} = 2F_{\mu\alpha} F_{\nu}^{\alpha} - \frac{1}{2} g_{\mu\nu} F_{\alpha\beta} F^{\alpha\beta}, \quad d \star F = 0.$$



- ❖ Descretize PDEs chebyshev x fourier
- ❖ Solve with Spectral Methods
(exponential convergence)

Ansätze

$$ds_{sol}^2 = \frac{1}{(1-r^2)^2} \left\{ A(r, x) d\tau^2 + \frac{4G(r, x)dr^2}{2-r^2} + r^2(2-r^2) \left[\frac{4C(r, x)}{2-x^2} \left(dx + \frac{H(r, x)dr}{r} \right)^2 + B(r, x)(1-x^2)^2 d\phi^2 \right] \right\}$$

$$\tilde{A}_\tau^{sol} = -i r D(r, x) d\tau$$

$$ds_{BH}^2 = \frac{1}{(1-r^2)^2} \left(d\tau^2 r^2 A(r, \theta) f_{BH}(r) + R^2 \left(\frac{4dr^2 G(r, \theta)}{f_{BH}(r)} + C(r, \theta)(d\theta + 2rdrH(r, \theta))^2 + d\phi^2 B(r, \theta) \sin^2 \theta \right) \right)$$

$$f_{BH}(r) = (1-r^2)^2 - Q^2(1-r^2)^3 + R^2(3-3r^2+r^4)$$

$$\tilde{A}_\tau^{BH} = -ir^2 D(r, \theta) d\tau$$

Boundary Conditions:

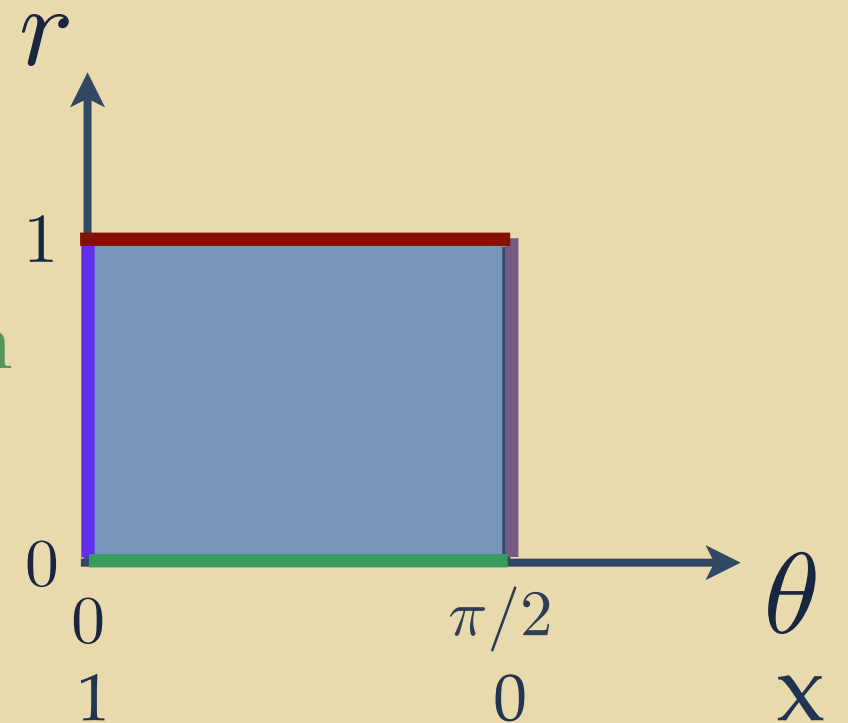
♣Regularity at Axes of Symmetry

hor / origin
 equator
 pole

♣At infinity $A = G = C = B = 1$

$$H = 0$$

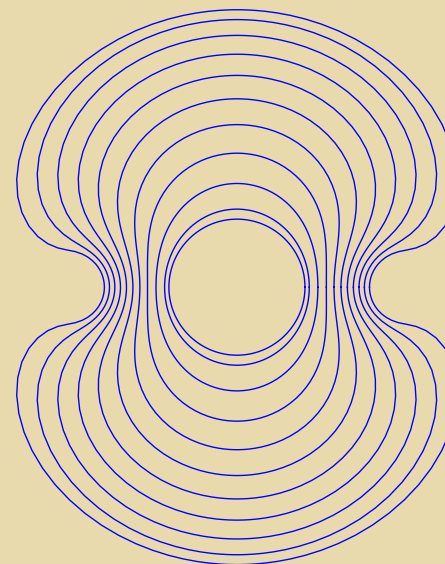
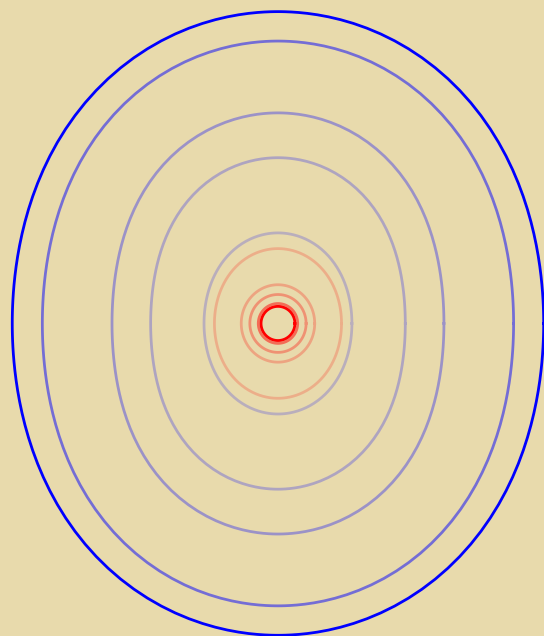
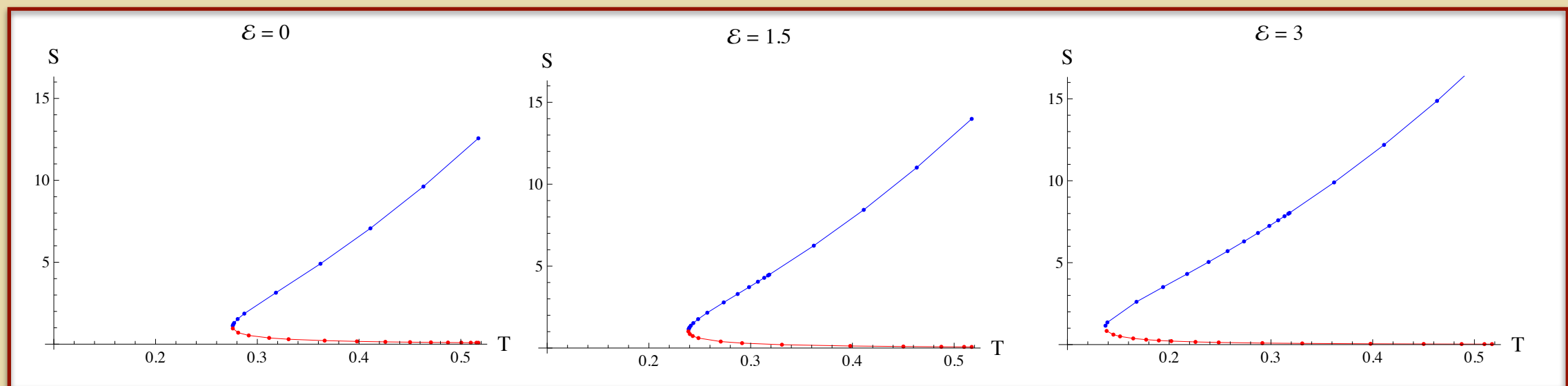
$$D = \mathcal{E} \cos \theta$$



Black Hole Polarization

What happens to the shape of the horizon when we change \mathcal{E} and T ?

$$S = \frac{\mathcal{A}}{4G_N} = \frac{\pi R^2}{G_N} \int_0^{\frac{\pi}{2}} d\theta \sin \theta \sqrt{C(0, \theta) B(0, \theta)}$$



Free Energy

$$T_{\mu\nu} = \frac{2}{\sqrt{h}} \frac{\delta S}{\delta h^{\mu\nu}} = \frac{1}{8\pi G_N} (K_{\mu\nu} - K h_{\mu\nu} + G_{\mu\nu} - 2h_{\mu\nu})$$

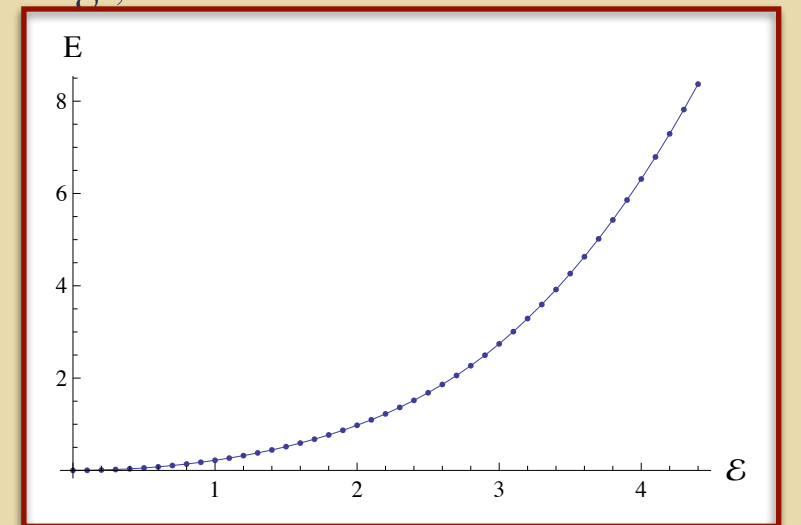
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$$E = \int d\Omega_2 T_t^t$$

e.g., for the soliton...

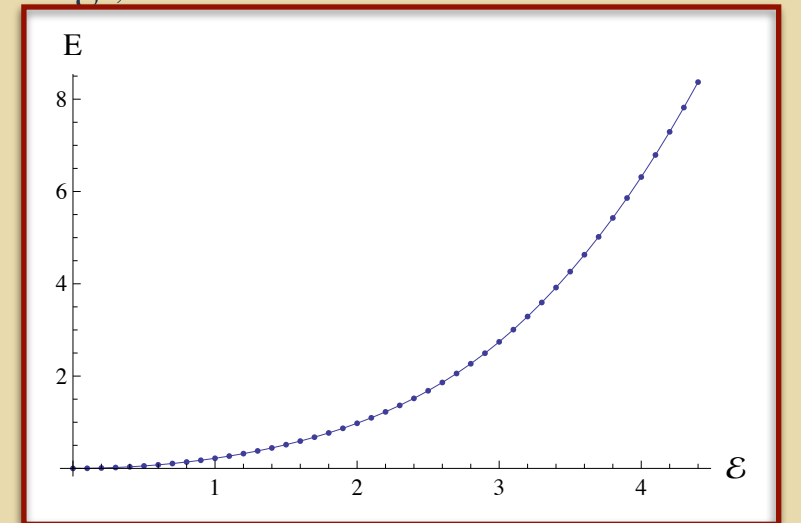


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$$\rho(\theta) d\Omega_2 = \frac{1}{4\pi G_N} \int \star F|_{r=1}$$

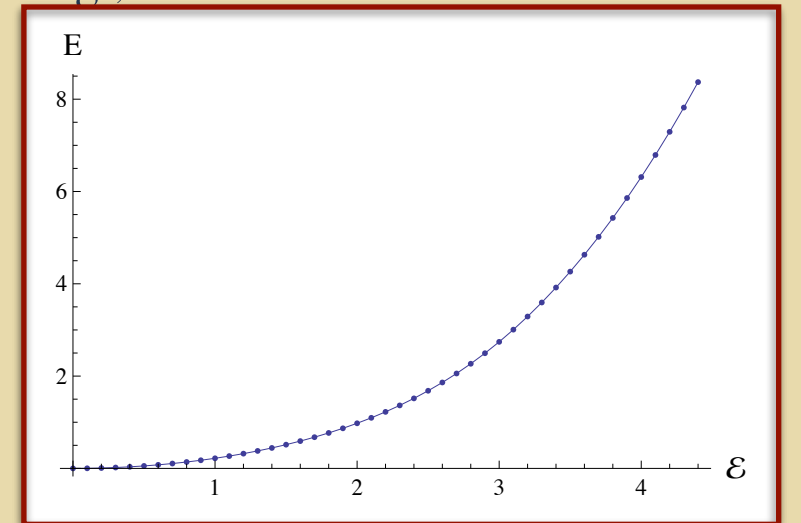


Free Energy

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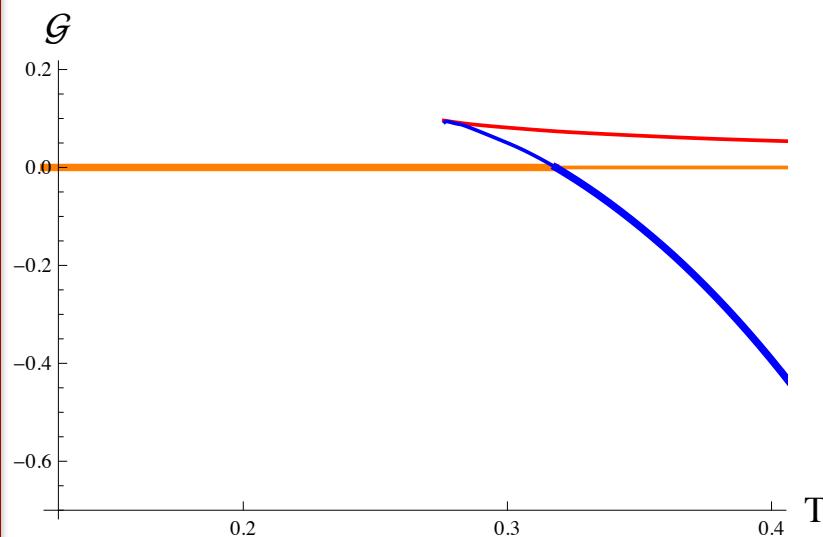
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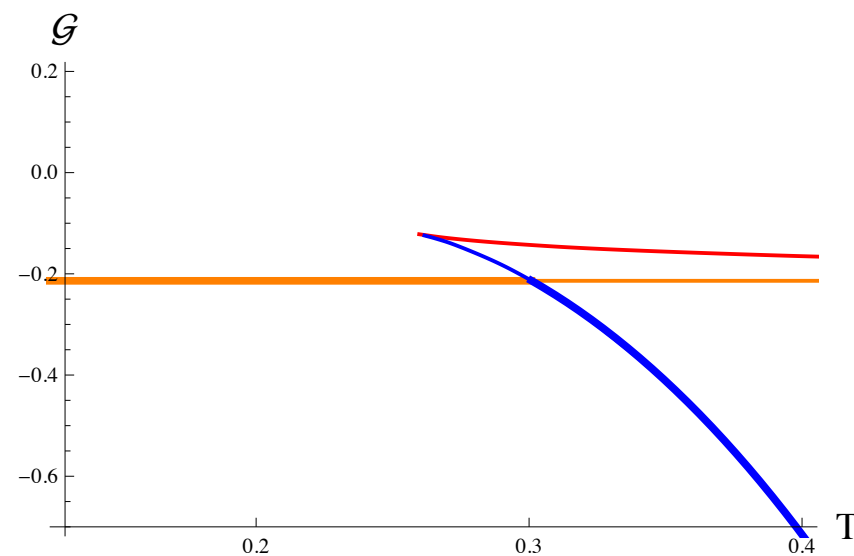


$$\Rightarrow \mathcal{G} = E - TS - 4\pi \int_0^{\pi/2} d\theta \sin \theta \rho(\theta) \mathcal{E} \cos \theta$$

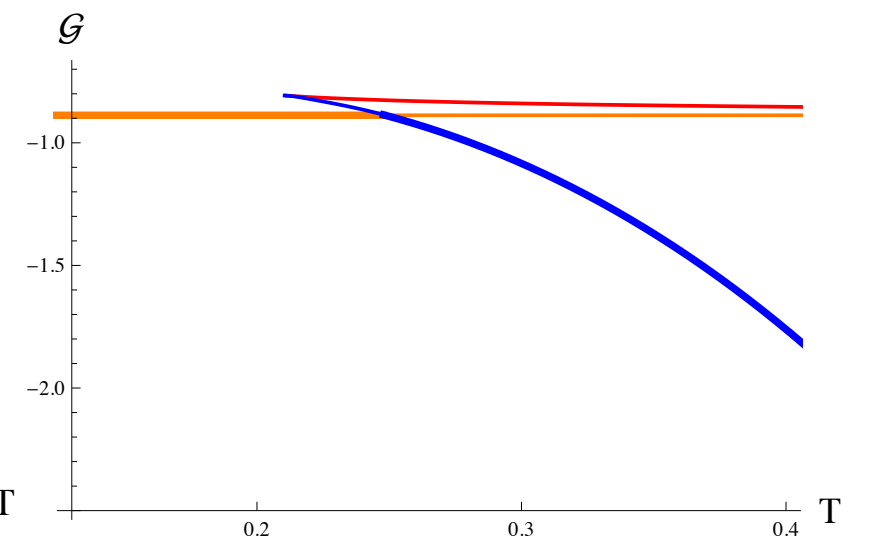
$\mathcal{E} = 0$



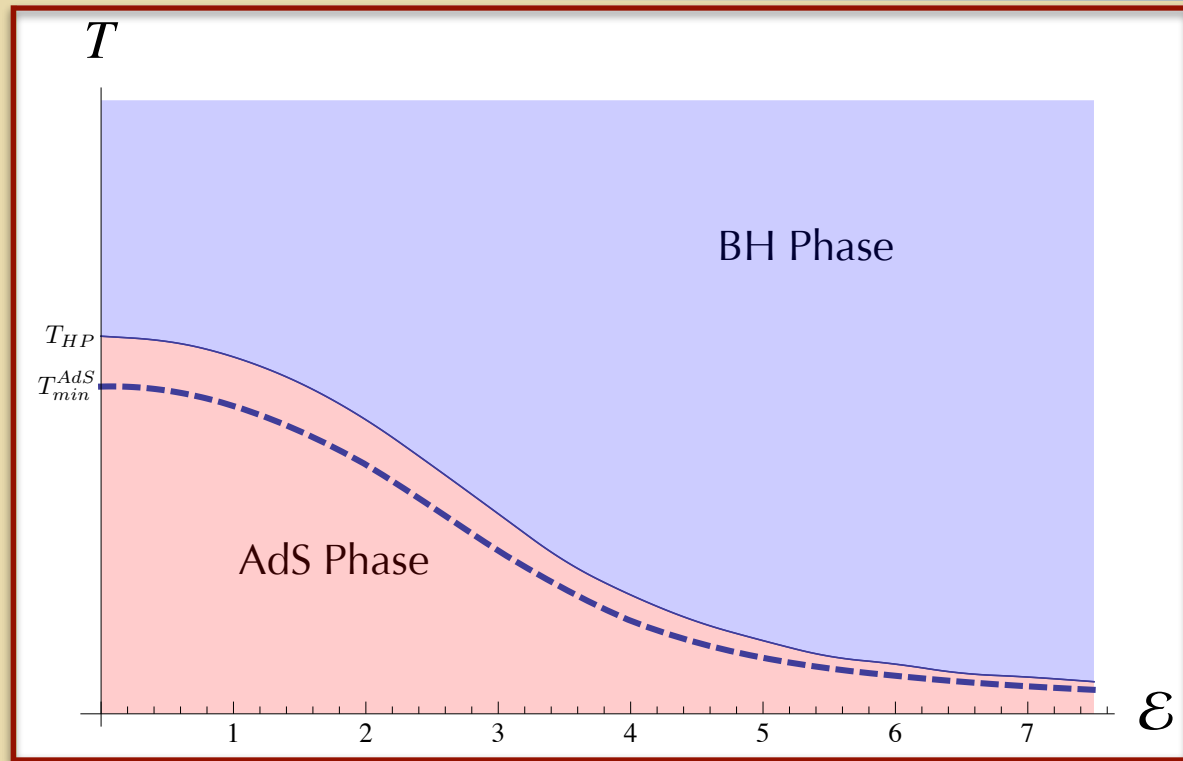
$\mathcal{E} = 1$



$\mathcal{E} = 2$

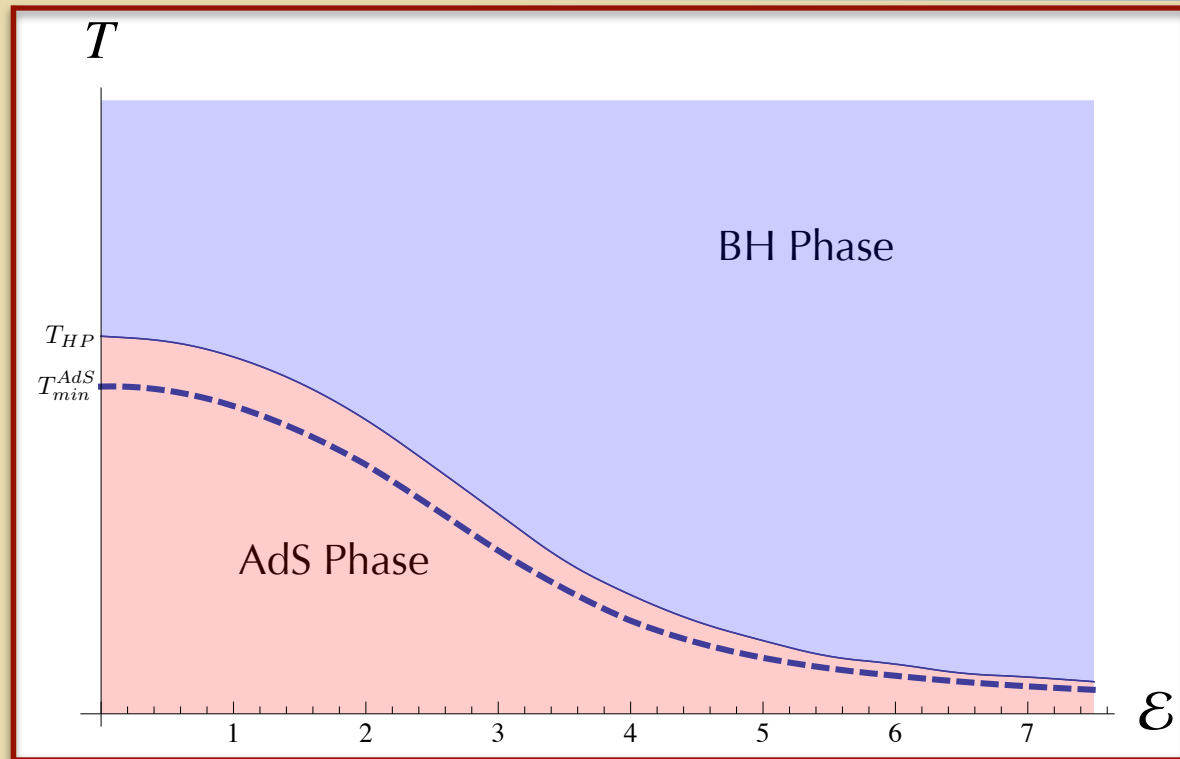


Phase diagram



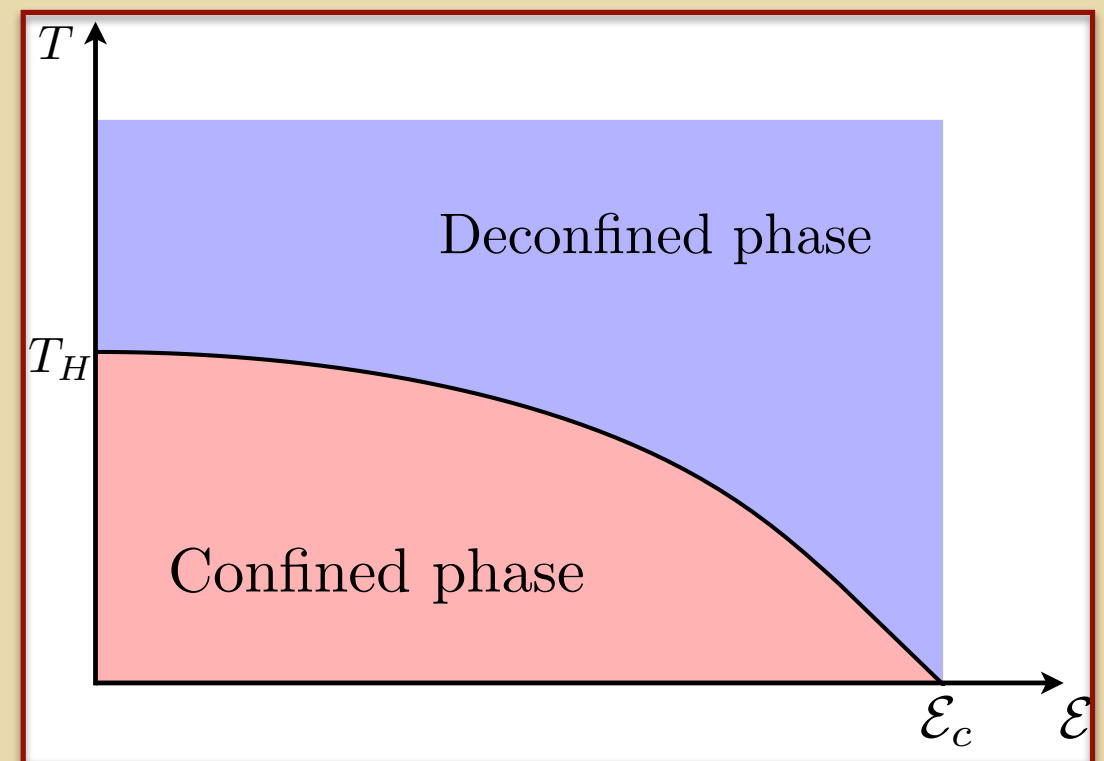
- Strong coupling picture of some dual theory

Phase diagram

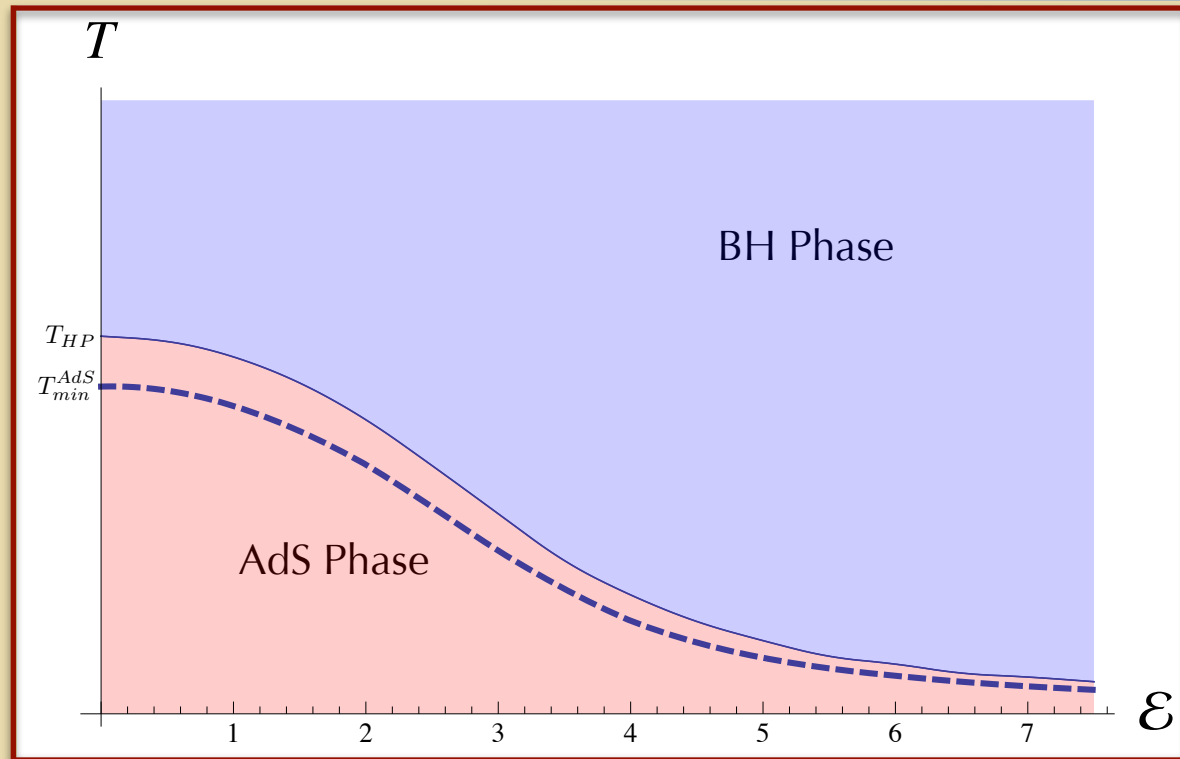


- Strong coupling picture of some dual theory

- ? Try looking at the partition function of free Bosons on a sphere to get weak coupling picture

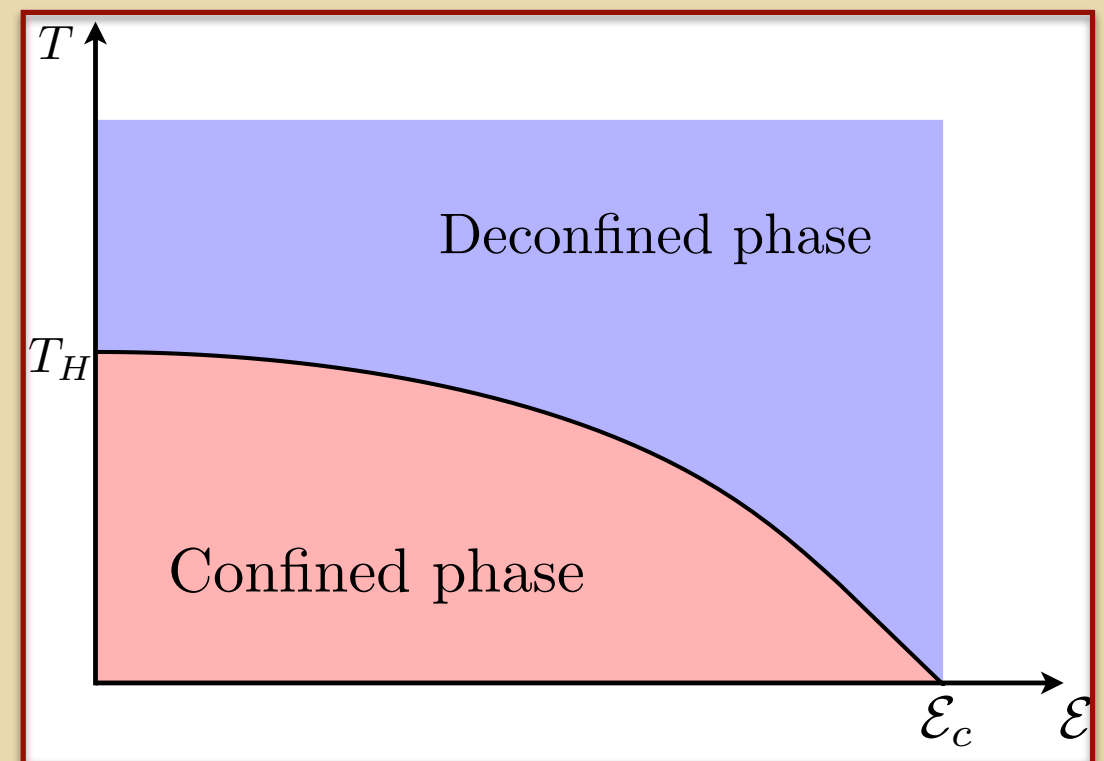


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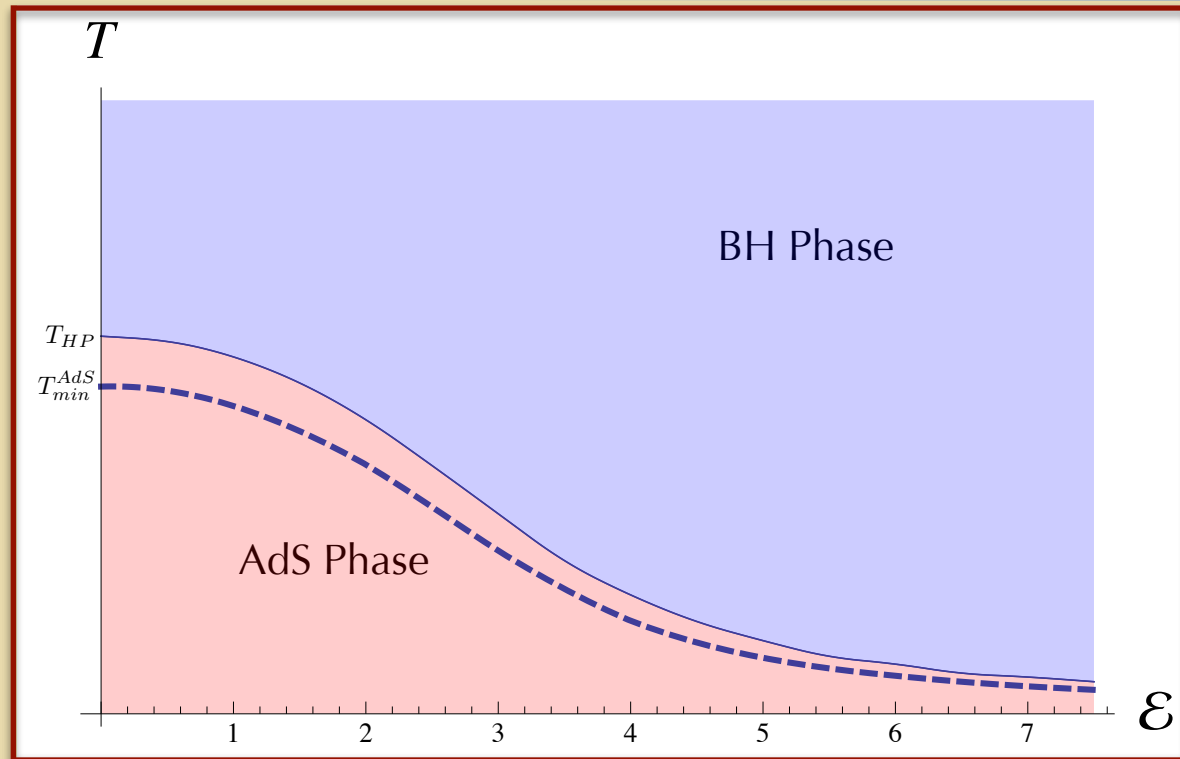


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maximum electric field

- Strong coupling picture of some dual theory
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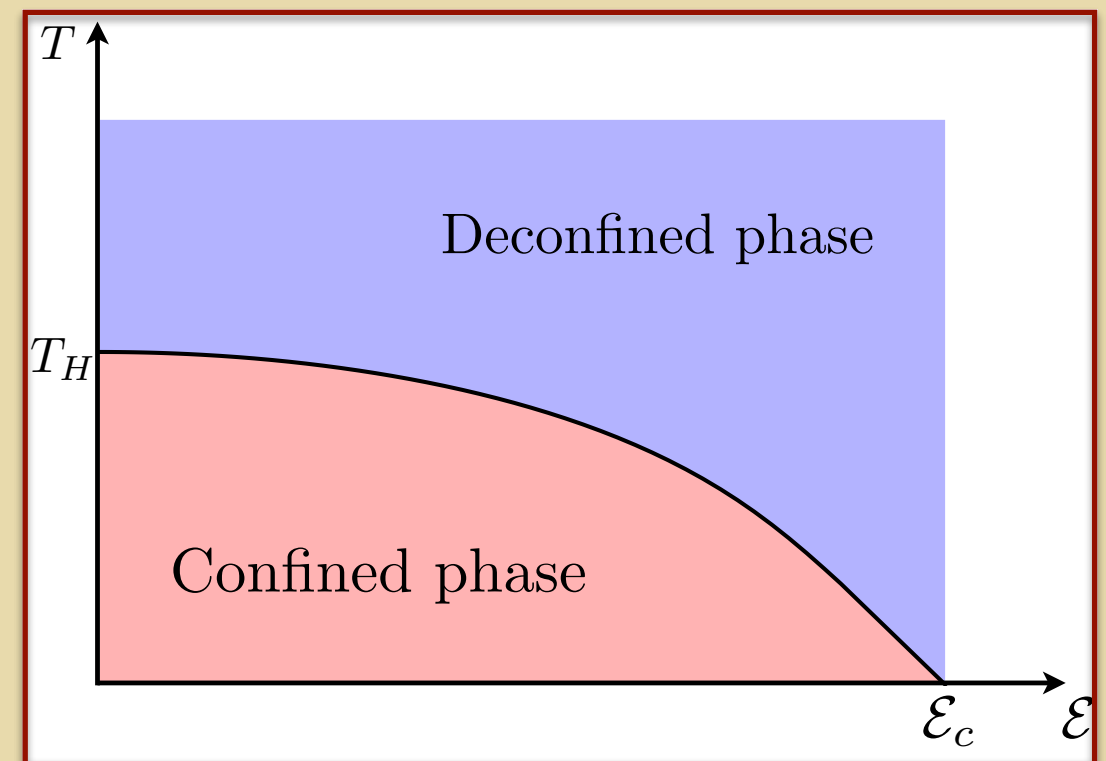


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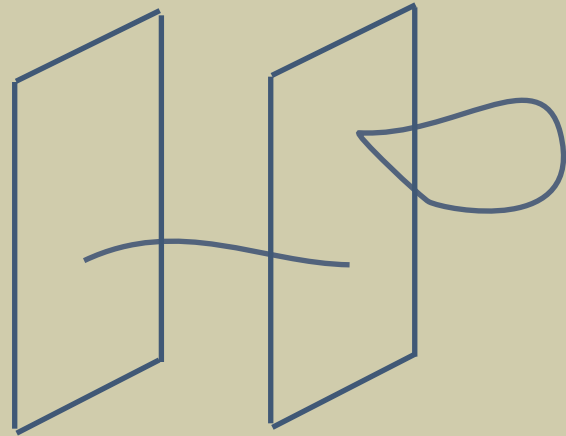


What is the correct gauge / gravity description for polarized black holes?

Current Work: ABJM

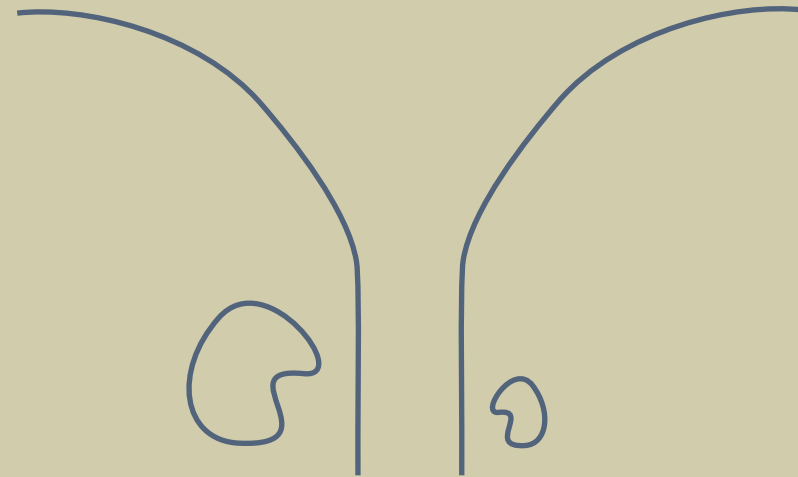
[Aharony, Berenstein, Jafferis, Maldacena 2008]

A precise dual of BH polarization is deformed 3 d ABJM theory



ABJM

M2
branes

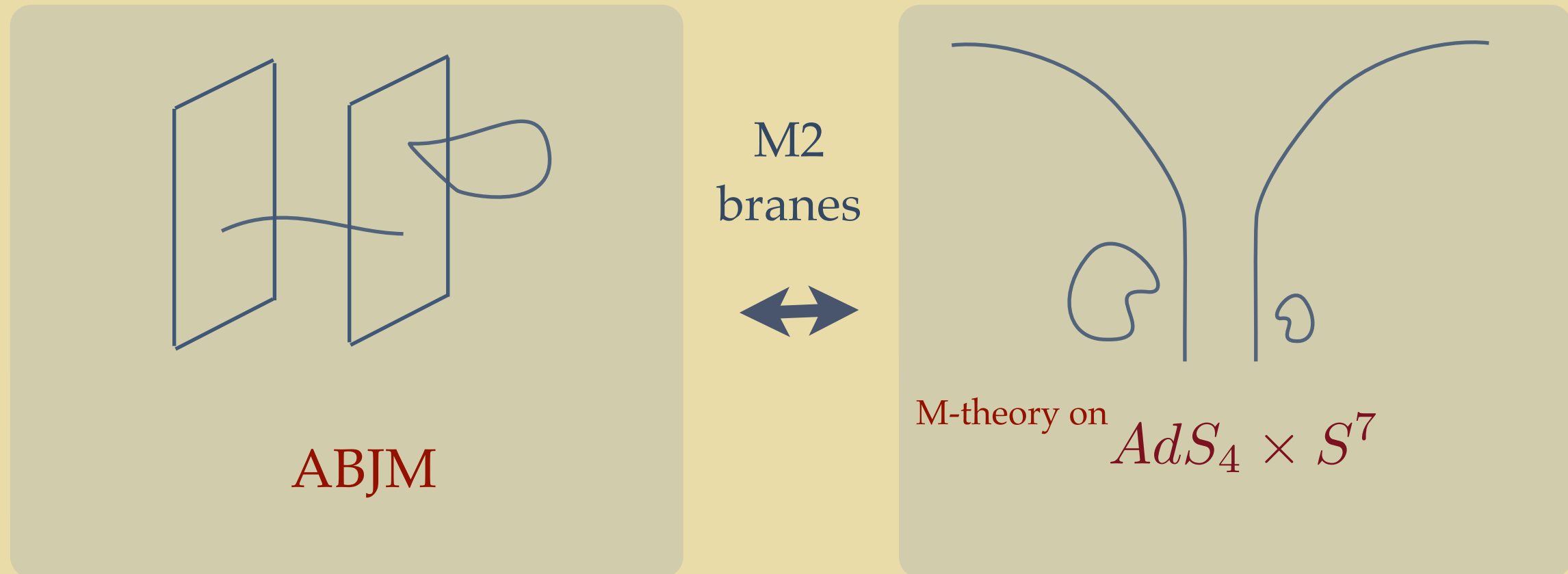



M-theory on $AdS_4 \times S^7$

Current Work: ABJM

[Aharony, Berenstein, Jafferis, Maldacena 2008]

A precise dual of BH polarization is deformed 3 d ABJM theory



$AdS_4 \times S^7$  4 d gauged SUGRA that can be truncated to include

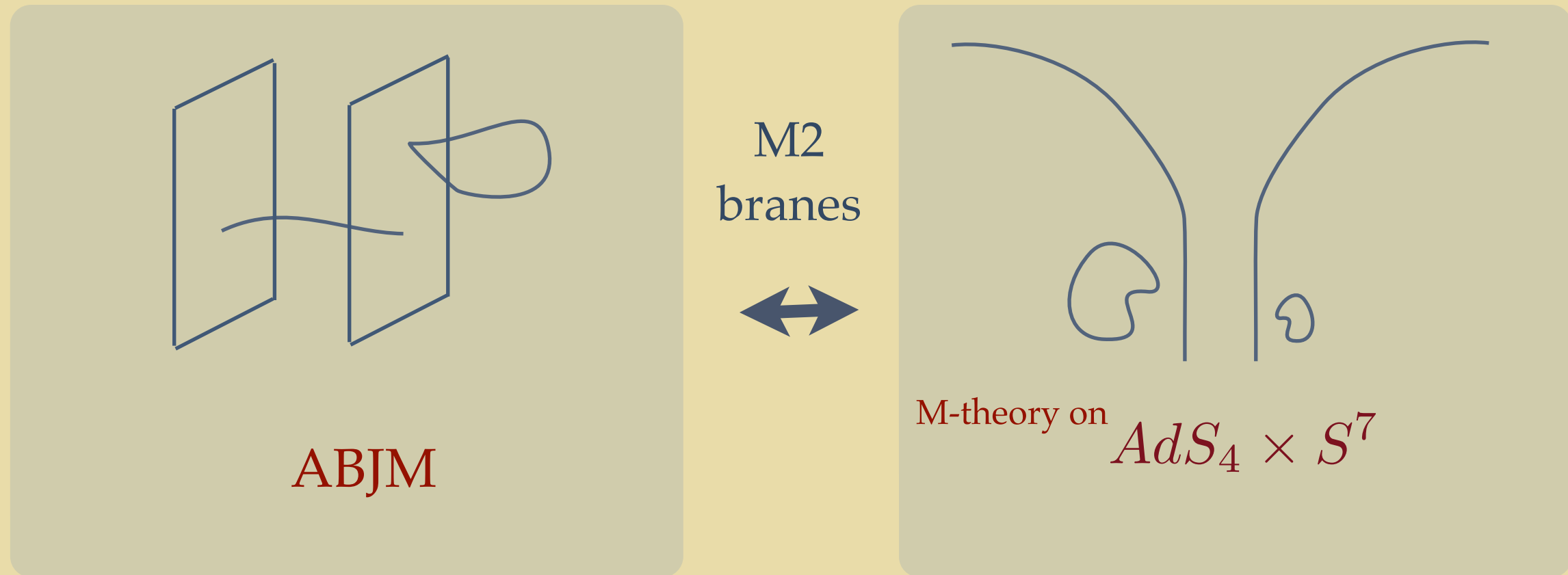
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[Cvetič, Duff, Hoxha et. al. 1999]

Non-normalizable mode

Current Work: ABJM [Aharony, Berenstein, Jafferis, Maldacena 2008]

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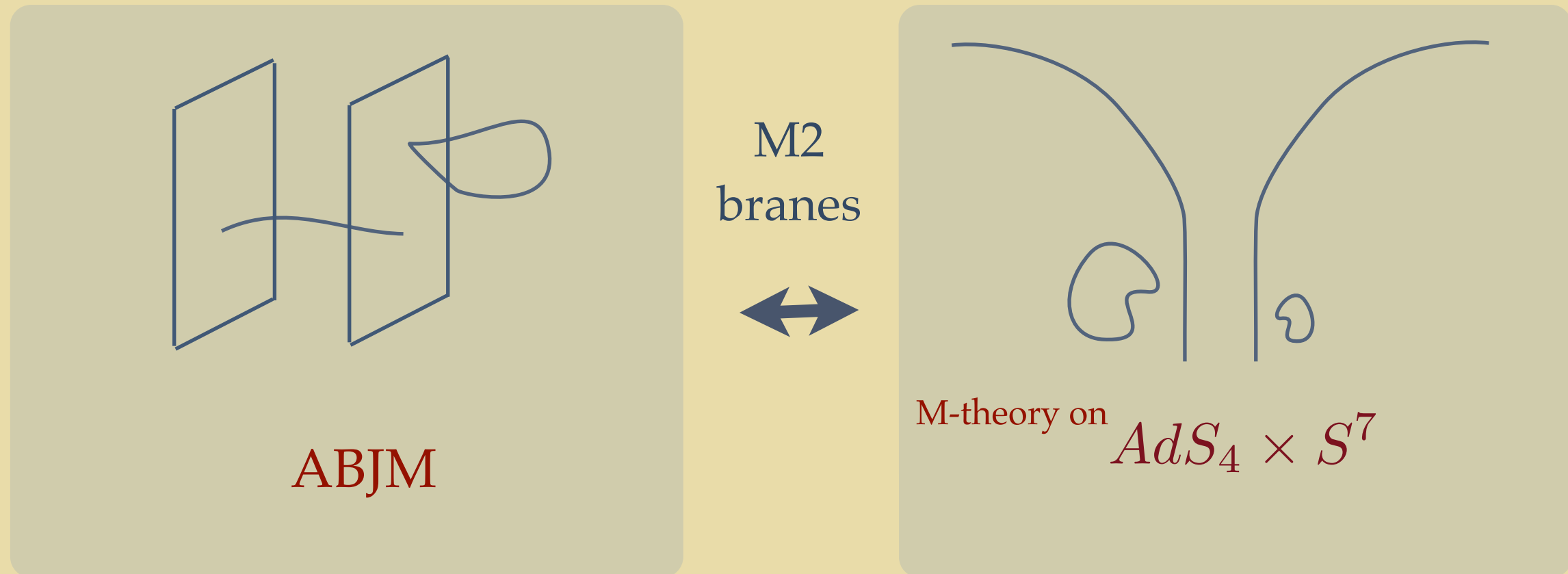
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[Cvetič, Duff, Hoxha et. al. 1999] Maximum electric field!

Concrete Realization of the gauge/gravity duality!

[Itzhaki, Maldacena, Sonnenschein, Yankielowicz '98]

Current/ Future Work

- ♣ study dynamical stability of BH
- ♣ Can deformation of ABJM be simulated on a computer?
- ♣ Condensed Matter...

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Thank You