

An inspiral-merger-ringdown waveform model for compact binaries on eccentric orbits

LIGO Document: P1600186

Eliu Huerta

National Center for Supercomputing Applications (NCSA)
University of Illinois at Urbana-Champaign

Collaborators

Gabrielle Allen, Bhanu Agarwal, Daniel George, Hsi-Yu Schive, Ed Seidel (NCSA)

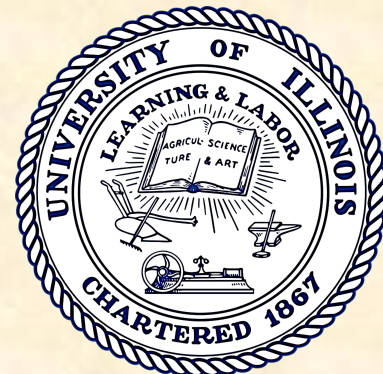
Harald Pfeiffer and Prayush Kumar (CITA)

Tony Chu (Princeton), Michael Boyle and Lawrence Kidder (Cornell)

Daniel Hemberger and Mark Scheel (TAPIR), Bela Szilagyi (JPL)



21st International Conference
on General Relativity and Gravitation
Columbia University, New York



Outline

- ❖ Motivation
- ❖ Waveform model construction
- ❖ Applications
- ❖ Future work

Motivation

- Gravitational wave astrophysics is already revolutionizing our understanding of the Universe [GW Highlights Sessions on Tuesday]
- Near future: accurate census of the mass and angular momentum distribution of compact sources; constraints on their channels of formation and evolution, and the environments where they reside

Extend the science reach of gravitational wave astrophysics

- Eccentric compact binaries may form in dense stellar environments and retain eccentricity during their lifetime [*Fabian (1975), Pooley (2003), O'Leary (2009), East & Pretorius (2013), Lee et al (2010), D. Tsang (2013), L. Wen (2003), D. Tsang (2013)*]
- Detecting these sources will provide unique insights about compact object populations in globular clusters and galactic nuclei [*Maccarone et al (2007), Irwin et al (2010), Strader et al (2012), Antonini (2014), Hopman et al (2006), Rodriguez et al (2015)*]

Motivation

- ⦿ The detection of GW150914 made evident that we needed inspiral-merger-ringdown (IMR) waveform models to constrain the residual eccentricity of gravitational waves [**Ian Hinder (Monday), Adam Lewis (Thursday)**, *Arun et al 2009, Yunes et al (2009), Hinder et al 2010, Huerta and Brown (2012), Huerta et al (2014)*]
- ⦿ We have developed a model that is suitable for this analysis, under the assumption that the binary components are non-spinning (Huerta, Kumar, et al. In review) [LIGO-P1600186]
- ⦿ The corresponding manuscript was submitted for LIGO's internal review on June 08. It has been reviewed and accepted.

Structure of the *ax* model

PN-based
inspiral



Improved inspiral:
Self force +
Black Hole
Perturbation Theory

All known
eccentricity corrections
up to 3PN order.

Fluxes include
instantaneous, tails, tails-of-tails
contributions, and a contribution due to
non-linear memory [Arun et al (2009)]

Caveat: lacks accuracy
for systems with
asymmetric mass-ratios

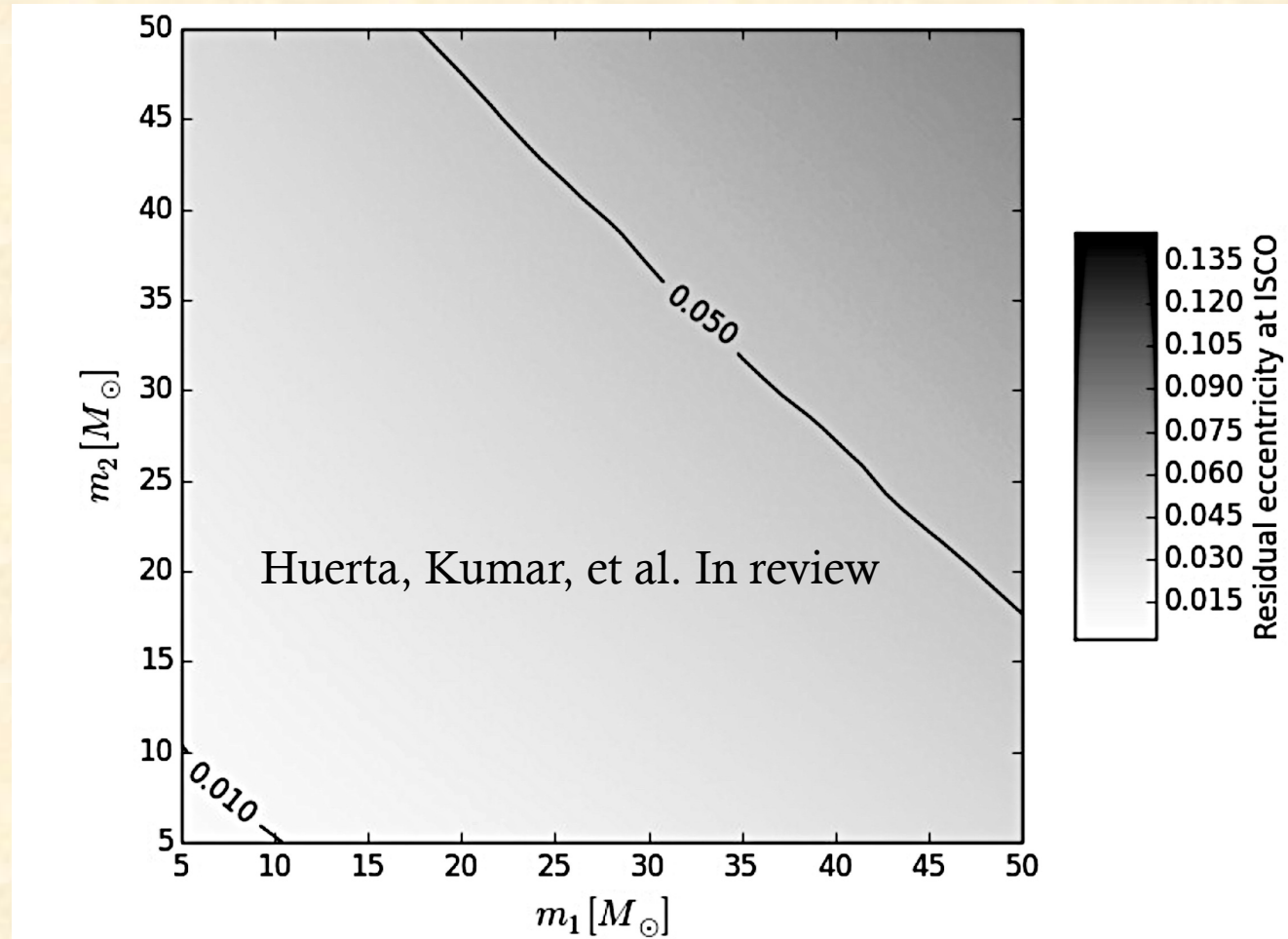
Flux of energy and binding energy
up to 6PN order including linear in
mass-ratio corrections [Fujita
(2012), Barusse et al (2012),
Damour et al (2013)]

Benefit: improves accuracy for
asymmetric
quasi-circular mass-ratio binaries

Eccentricity decay

BBH population with an initial eccentricity $e=0.3$ at a GW frequency of 15Hz.

Moderately eccentric binaries circularize prior to the merger event



Structure of the *ax* model

PN-based
inspiral



Improved inspiral:
Self force +
Black Hole
Perturbation Theory



Quasi-circular
merger waveform

All known corrections
up to 3PN order.

Fluxes include
instantaneous terms, tails,
tails-of-tails contributions
and non-linear memory

Caveat: lacks accuracy
for systems with
asymmetric mass-ratios

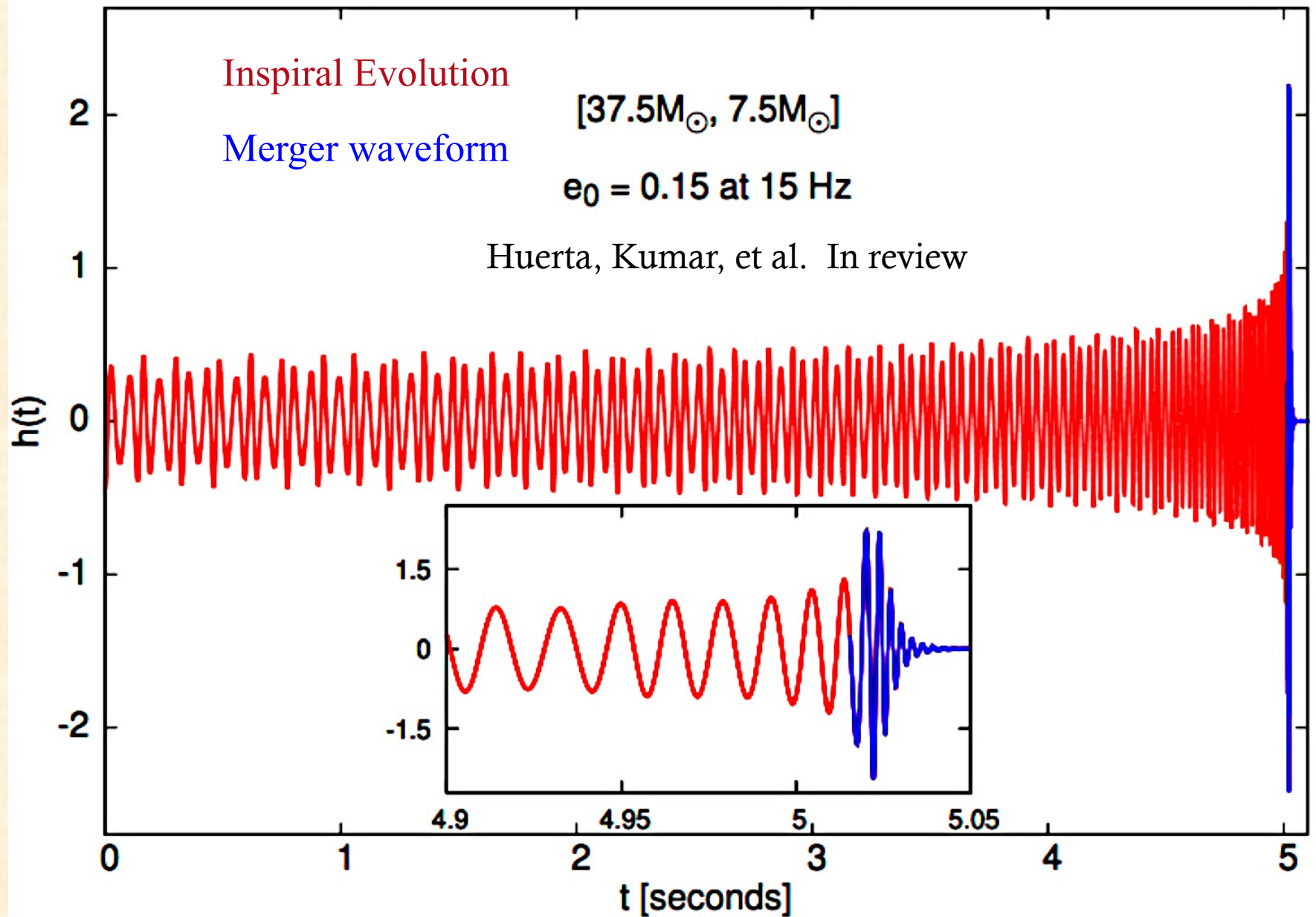
Flux of energy and
binding energy up to
6PN order including
linear in mass-ratio
corrections

Benefit: improves
accuracy for
asymmetric
mass-ratio binaries

Implicit Rotating
Source (IRS) formalism
calibrated with numerical
relativity simulations up to
mass-ratio 10 [Baker et al
(2008), Kelly et al (2010)]

Caveat: very accurate only
in the vicinity of the light-
ring

Complete waveform

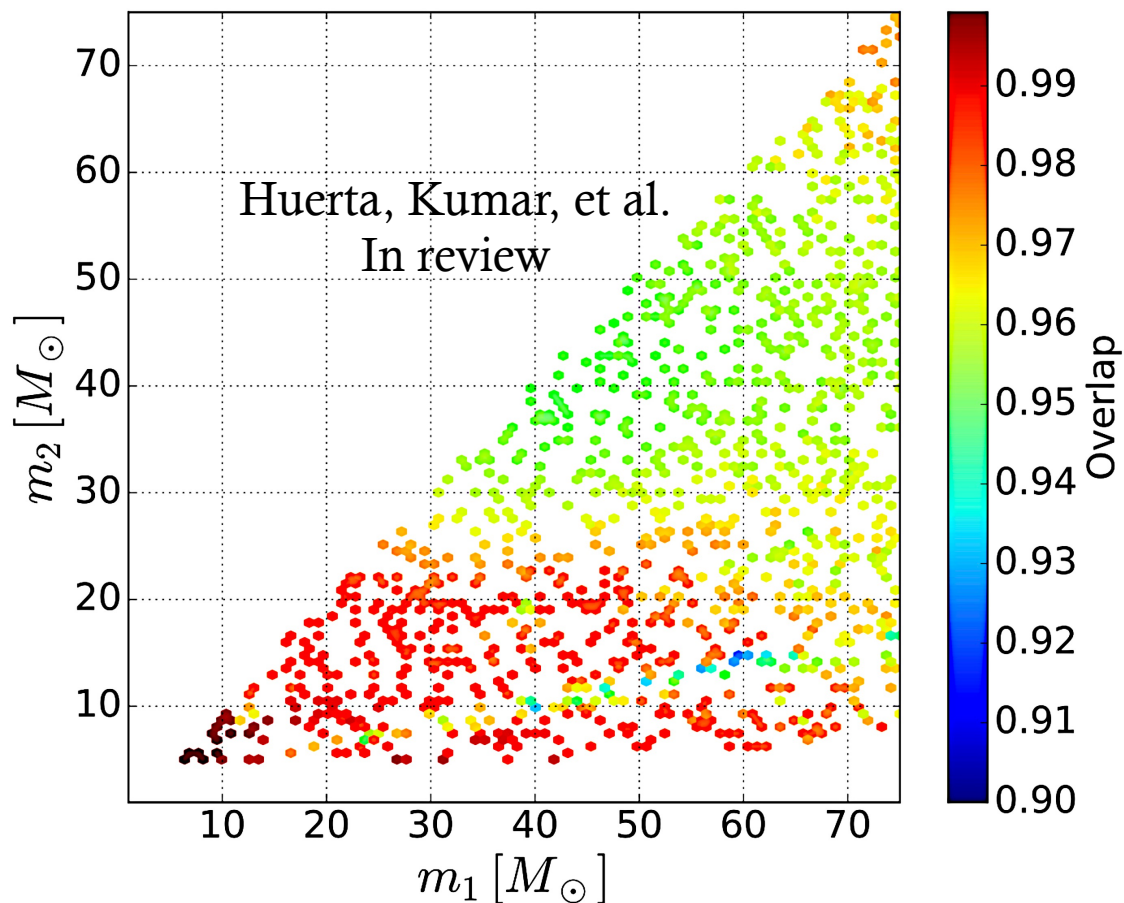


Comparison to state-of-the-art quasi-circular waveforms in the zero eccentricity limit

PSD: mid-aLIGO

Initial filtering frequency: 25Hz

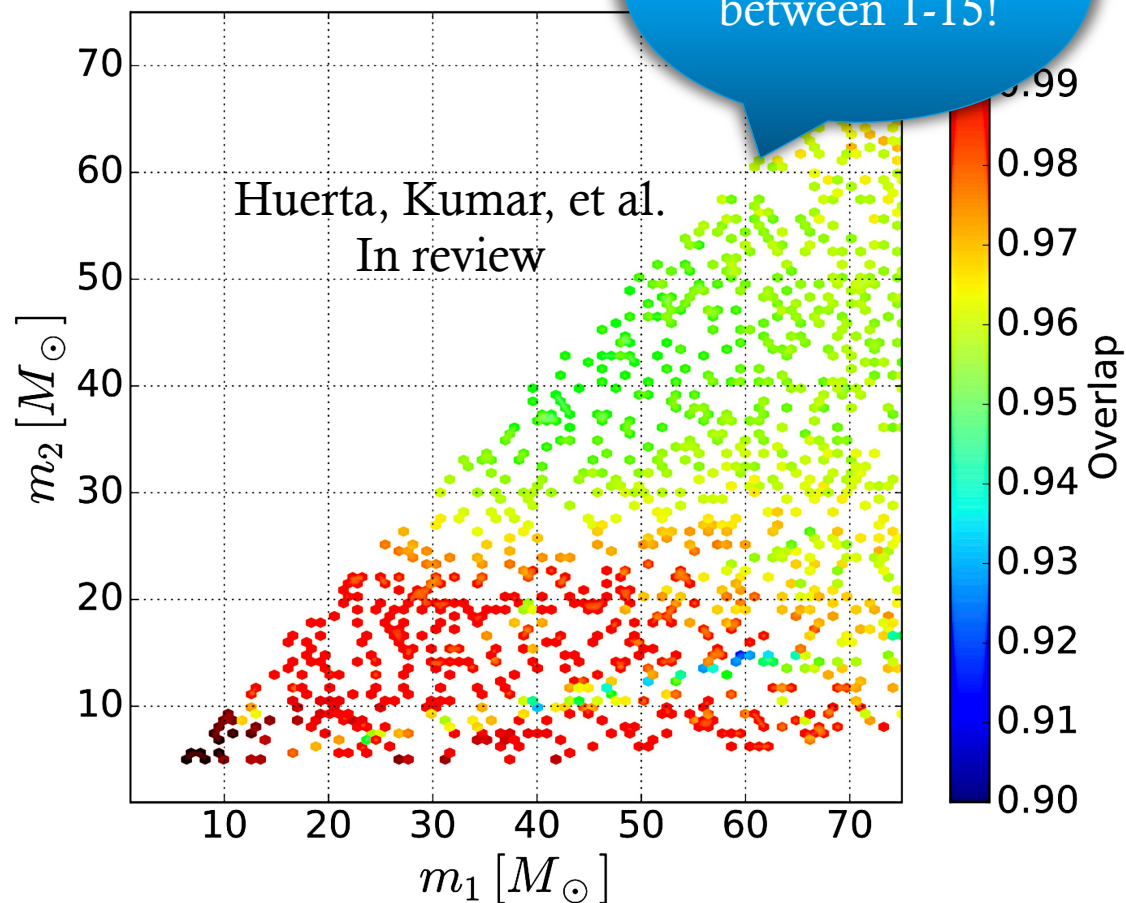
IMR eccentric model agrees
well with the effective-one-
body model (EOBNRv2) over a
wide range of the BBH
parameter space accessible to
aLIGO



Comparison to EOBNRv2 in the zero eccentricity limit

PSD: mid-aLIGO
Initial filtering frequency:
25Hz

IMR eccentric model agrees
well with EOBNRv2 over a
wide range of the BBH
parameter space accessible to
aLIGO



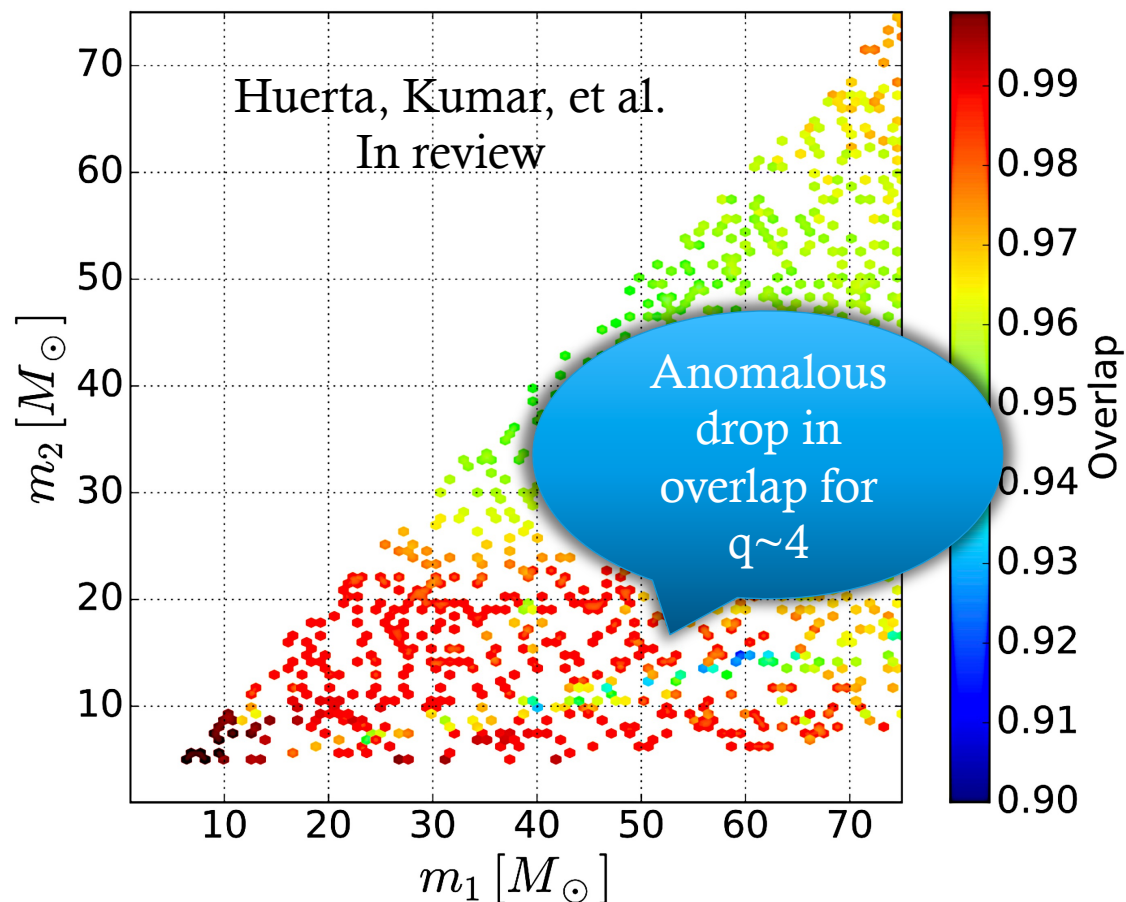
Comparison to EOBNRv2 in the zero eccentricity limit

PSD: mid-aLIGO

Initial filtering frequency:
25Hz

IMR eccentric model agrees
well with EOBNRv2 over a
wide range of the BBH
parameter space accessible to
aLIGO

Improved version of the
merger waveform using a
larger set of NR simulations

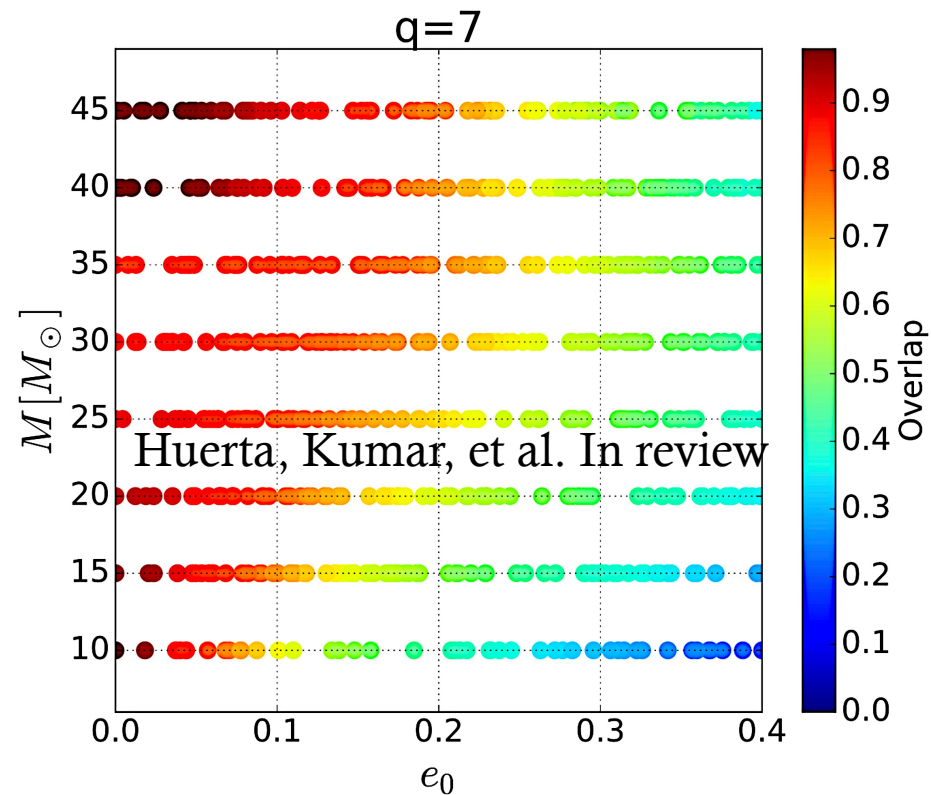
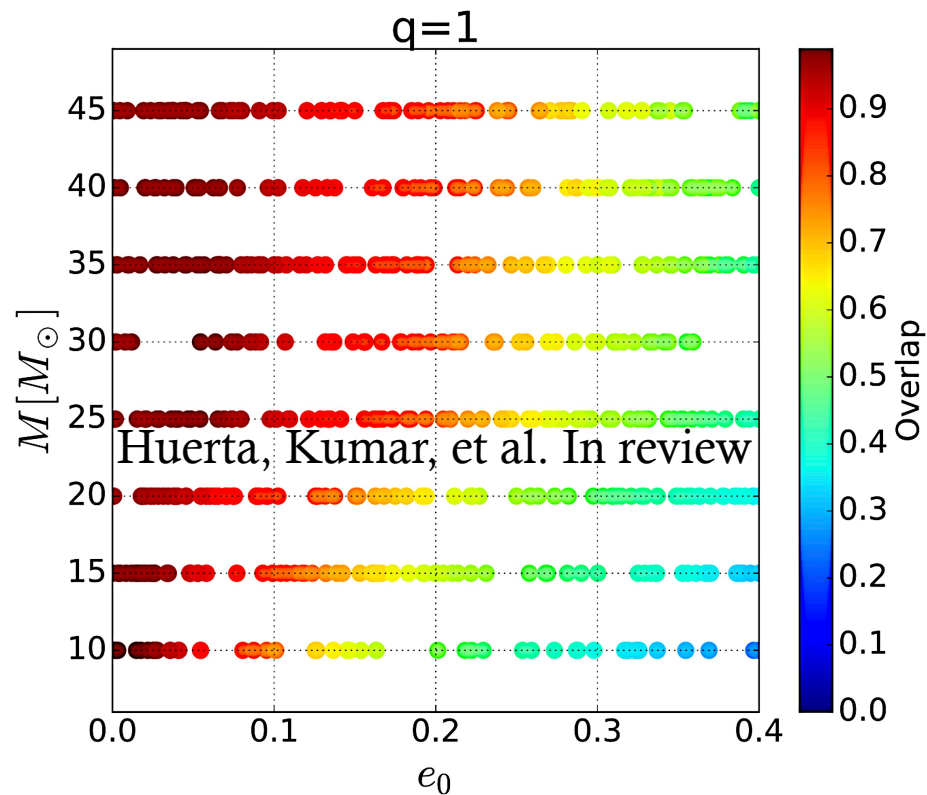


Applications

PSD: Zero Detuned High Power

Initial filtering frequency: 15Hz

Eccentricity of x-axis defined at a GW frequency of 15Hz



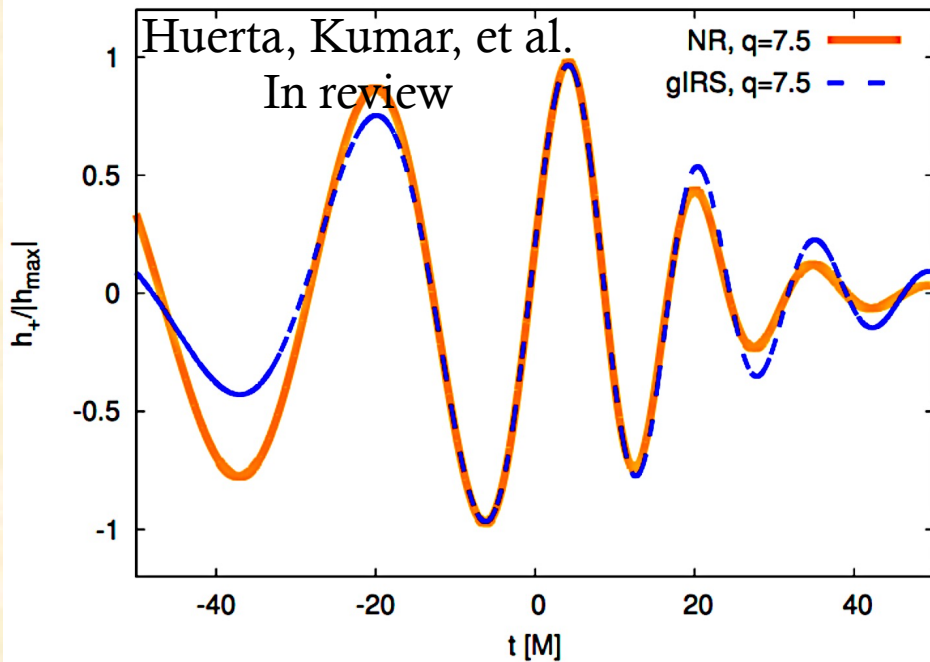
Improving the merger model

NCSA: Miguel Holgado and Erik Wessel

Cambridge: Alvin Chua and Chris Moore

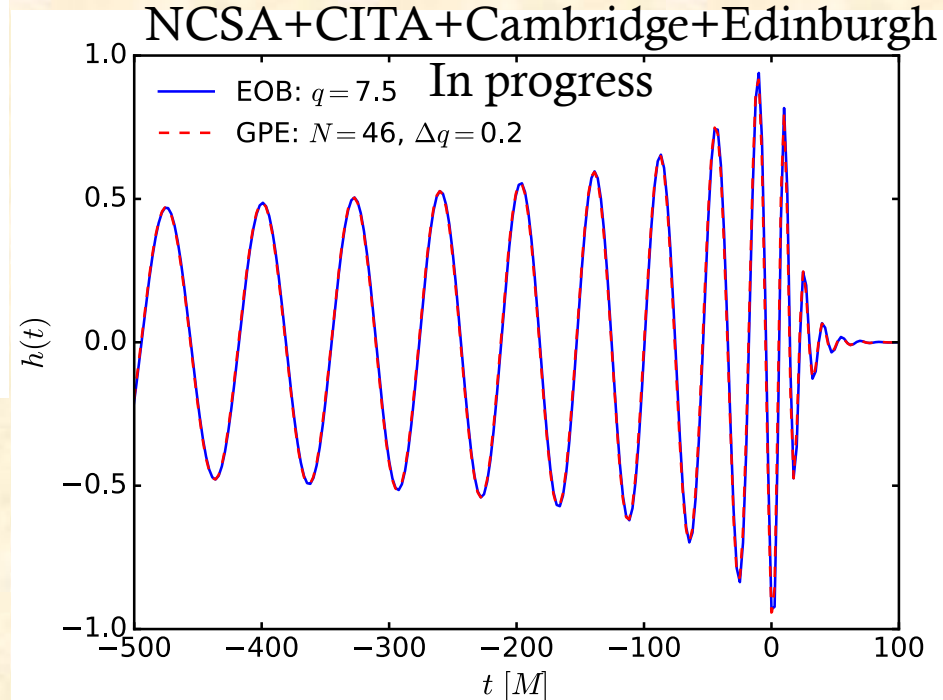
CITA: Harald Pfeiffer and Prayush Kumar

Edinburgh: Jon Gair



gIRS works very well *in the vicinity of the light-ring*

Our new approach works very well *several cycles before merger!*



Future work

- With Ian Hinder: quantify the accuracy of our IMR models using numerical relativity simulations for astrophysically motivated sources
- We will use our models to quantify how accurately we can constrain the residual eccentricity of new detections with aLIGO
- We are developing new tools to detect and characterize eccentric sources. Network of collaborators: NCSA (USA), CITA (Canada), Cambridge (UK), Edinburgh (UK), AEI (Germany) and ICTS (India)

Conclusions

- We have combined PN, self-force, black hole perturbation theory and numerical relativity to develop the first IMR model that can describe eccentric binaries with asymmetric mass-ratios
- We have shown that the model agrees well with EOBNRv2 in the zero eccentricity limit
- An improved version of the model is currently under construction to address two key issues:
 - Increase overlap with EOBNRv2 in the quasi-circular limit
 - Include spin of the binary components

Inspiral dominated systems

Power Spectral Density: Zero Detuned High Power

Initial frequency for filtering: 15Hz

Eccentricity on the x-axis defined at a GW frequency of 15Hz

TaylorT4 3.5PN vs *ax* model

