

TESTING SCALAR-TENSOR THEORIES OF GRAVITY WITH HIGHLY COMPACT NEUTRON STARS

RAISSA F. P. MENDES

Based on:

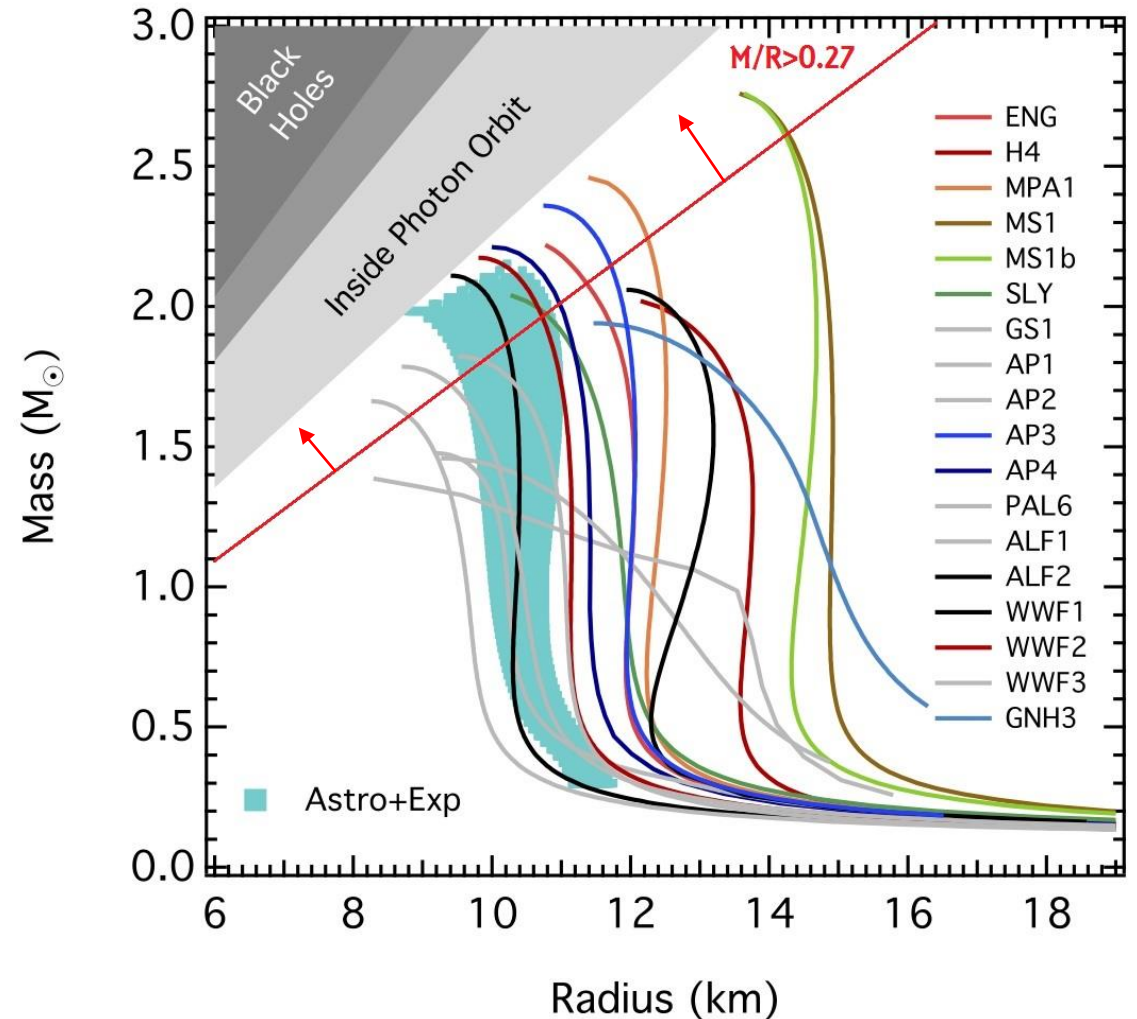
- R. F. P. Mendes, Phys. Rev. D 91, 064024 (2015), [arXiv:1412.6789](#).
- R. F. P. Mendes and N. Ortiz, Phys. Rev. D 93, 124035 (2016), [arXiv:1604.04175](#). (see also N. Ortiz's talk!)

A WORD ON NEUTRON STARS

- + 2500 pulsars in the Galaxy; 90% isolated.
- Precise masses for ~35 NS, from 1.17 to $2M_{\odot}$.
- Radius measurements for a dozen NS pinned down to the $9.9 - 11.2$ km range.
- Well described by perfect fluid with cold equation of state, $p = p(\rho)$.
- One-to-one relation: EoS $\leftrightarrow M/R$ diagram.
- Particularly relevant for us: “highly compact” neutron stars, satisfying

$$p_c > \frac{1}{3} \epsilon_c$$

which is achieved if $M/R \gtrsim 0.27$.



SCALAR-TENSOR THEORIES OF GRAVITY

- Natural, mathematically consistent and simple alternative to GR.
- Tractable: full nonlinear numerics (Barausse et al. 2013, Palenzuela et al. 2014, Shibata et al. 2014)

- Jordan frame:

$$S = \frac{1}{16\pi} \int d^4x \sqrt{-\tilde{g}} \left[F(\Phi) \tilde{R} - Z(\Phi) \tilde{g}^{\mu\nu} \partial_\mu \Phi \partial_\nu \Phi \right] + S_m[\Psi_m; \tilde{g}_{\mu\nu}]$$

$$g_{\mu\nu} = F(\Phi) \tilde{g}_{\mu\nu} = a(\phi)^{-2} \tilde{g}_{\mu\nu}$$

$$\phi = \int d\Phi \left[\frac{3}{4} \frac{F'^2(\Phi)}{F^2(\Phi)} + \frac{1}{2} \frac{Z(\Phi)}{F(\Phi)} \right]^{1/2}$$

- Einstein frame:

$$S = \frac{1}{16\pi} \int d^4x \sqrt{-g} \left[R - 2g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \right] + S_m[\Psi_m; a(\phi)^2 g_{\mu\nu}]$$

- Examples:

- Fierz-Jordan-Brans-Dicke theory: $F(\Phi) = \Phi$, $Z(\Phi) = \omega_{BD}/\Phi$.
- (massless) NMC scalar field: $F(\Phi) = 1 - \xi\Phi^2$, $Z(\Phi) = 1$.

SCALAR-TENSOR THEORIES OF GRAVITY

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- Field equations:

$$G_{\mu\nu} - 2\nabla_\mu \phi \nabla_\nu \phi + g_{\mu\nu} \nabla_\rho \phi \nabla^\rho \phi = 8\pi T_{\mu\nu}$$

$$\nabla_\mu \nabla^\mu \phi = -4\pi \alpha(\phi) T$$

$$\nabla_\mu T^{\mu\nu} = \alpha(\phi) T \nabla^\nu \phi$$

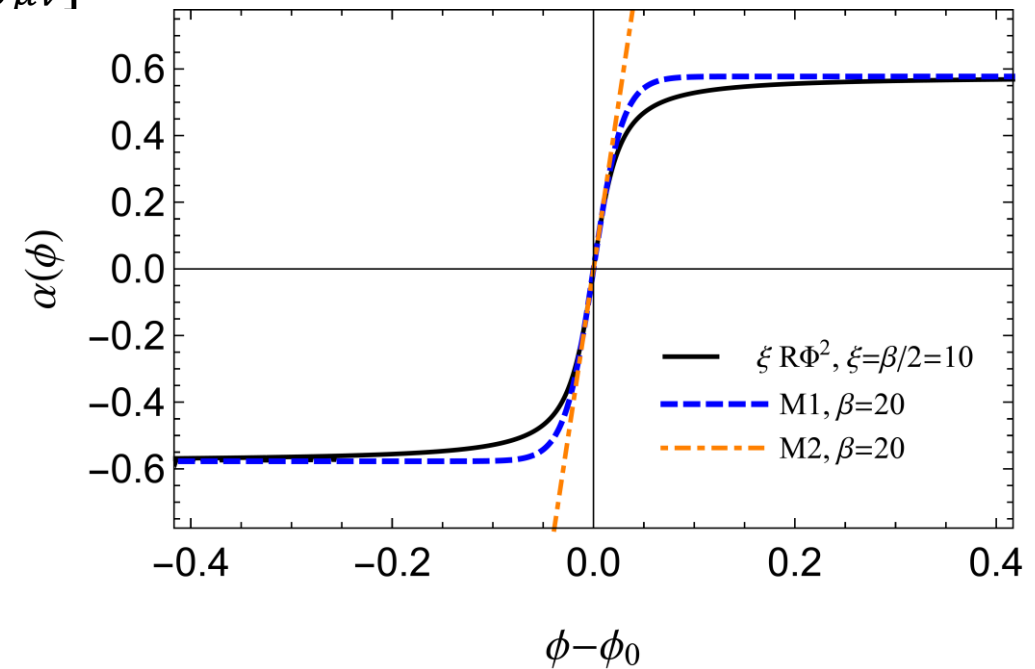
with $\alpha(\phi) := d \ln a(\phi) / d\phi$.

- Expand:

$$\alpha(\phi) = \alpha_0 + \beta_0(\phi - \phi_0) + O[(\phi - \phi_0)^2]$$

$\alpha_0 \sim \frac{1}{\sqrt{\omega_{BD}}} \sim 0$
(Solar System)

Responsible for the
most interesting effects!

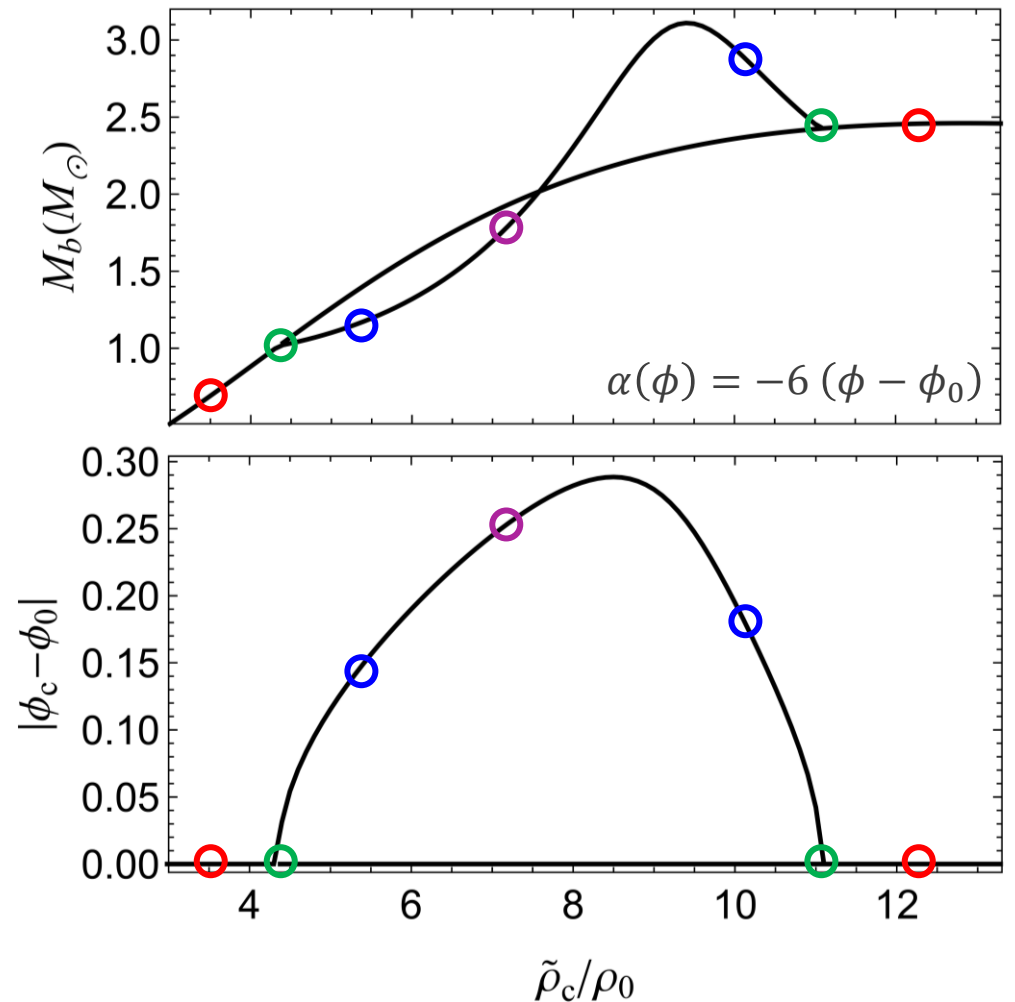
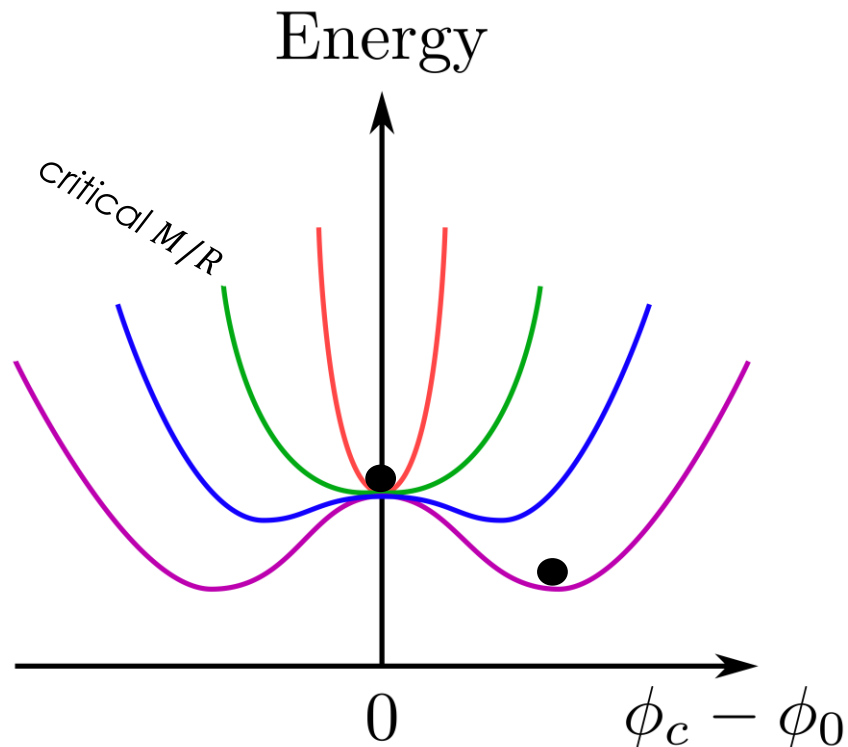


Model 1 (**M1**): $\alpha(\phi) = \frac{1}{\sqrt{3}} \tanh[\sqrt{3} \beta (\phi - \phi_0)]$
Model 2 (**M2**): $\alpha(\phi) = \beta (\phi - \phi_0)$

Differ only in $O[(\phi - \phi_0)^2]$ terms.

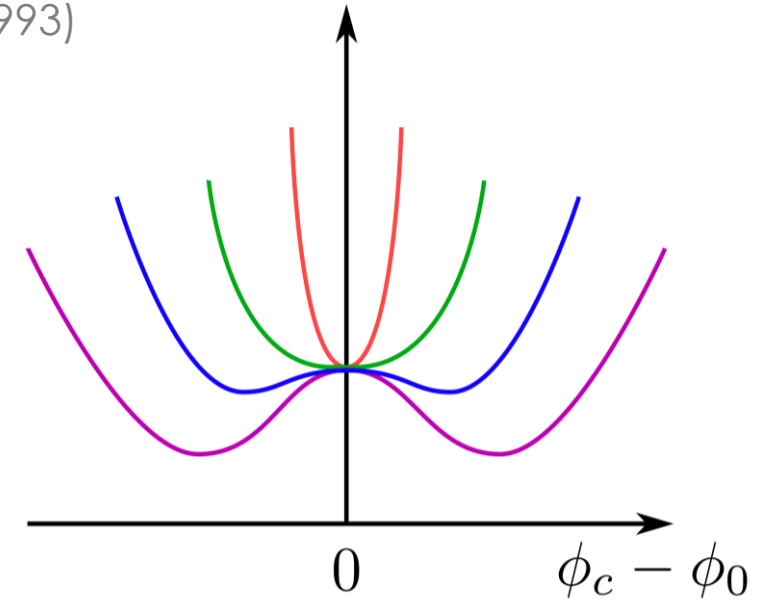
SPONTANEOUS SCALARIZATION OF NEUTRON STARS

- Nonperturbative strong-field effect (Damour & Esposito-Farèse, 1993)
- Phase transition ~ spontaneous magnetization



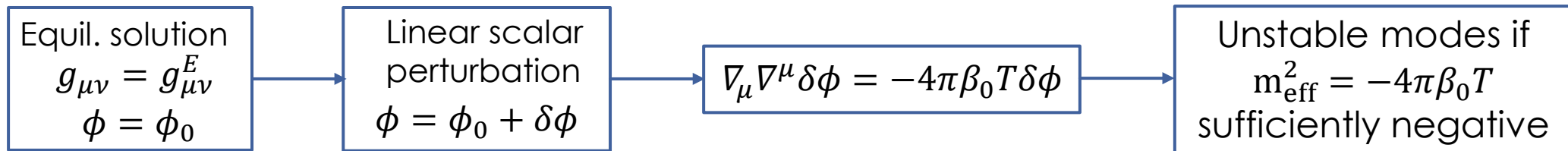
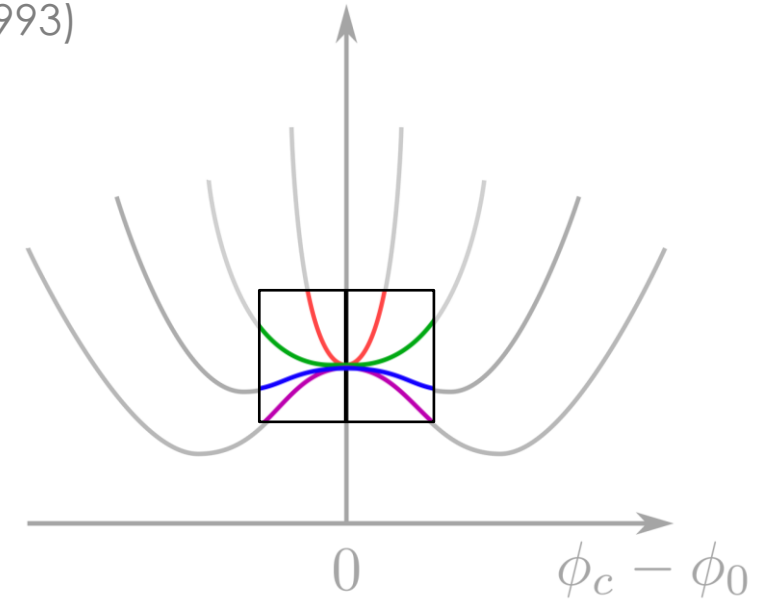
SPONTANEOUS SCALARIZATION OF NEUTRON STARS

- Nonperturbative strong-field effect (Damour & Esposito-Farèse, 1993)
- Strong field effects can be very important!
- Scalarization depends crucially on $\beta_0 = \alpha'(\phi_0)$.
 - Known to happen when $\beta_0 \lesssim -4.35$.
 - Dipolar radiation: PT rules out $\beta_0 \lesssim -4.5$ (Freire et al. 2012)
 - $\beta_0 > 0$ largely unexplored (and unconstrained)!



SPONTANEOUS SCALARIZATION OF NEUTRON STARS

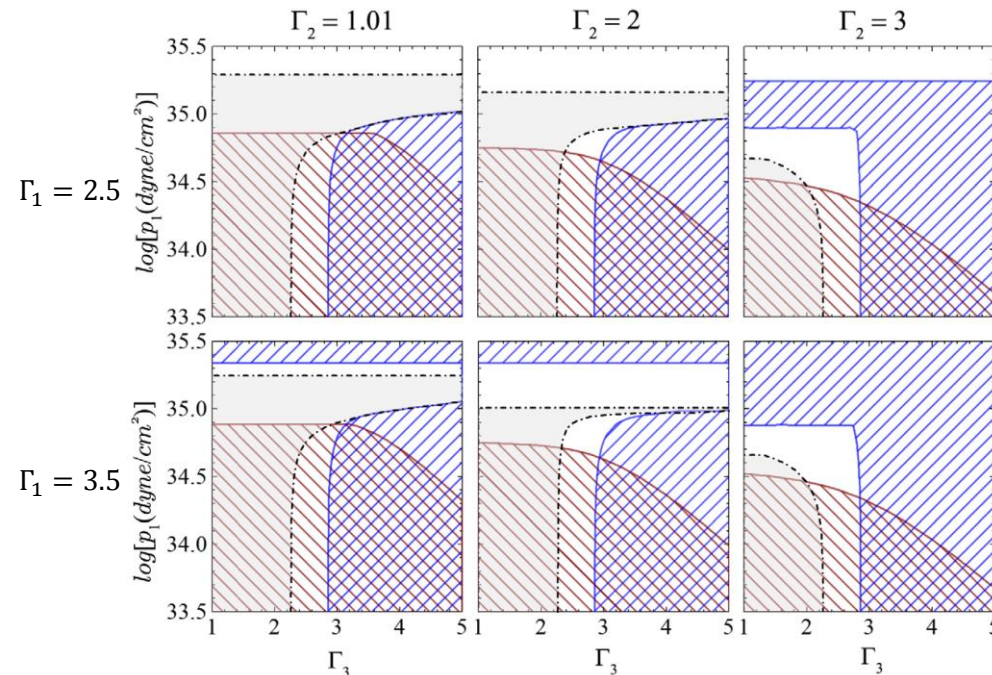
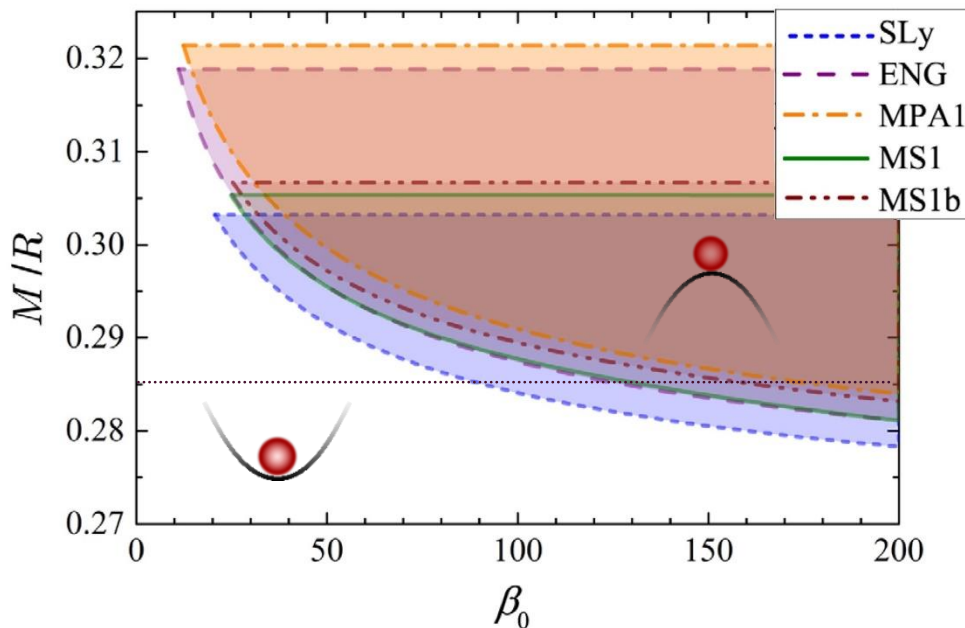
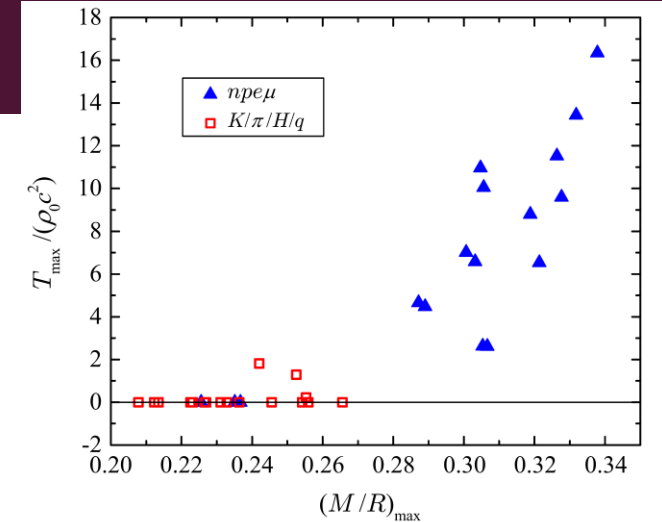
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 - $\beta_0 > 0$ largely unexplored (and unconstrained)!
- Insight from linear stability analysis (Harada 1997)



- $T > 0$ ($\Rightarrow p > \epsilon/3$) necessary for instability if $\beta_0 > 0$: **How “exotic” is this condition?**

$T > 0$ INSIDE “REALISTIC” NEUTRON STARS?

- Analysis of EOS in *parametrized* form & of *theoretical* models [Mendes, PRD91, 064024 (2015)]
- $T > 0$ inside hydrodynamically stable stars?
 - Yes! According to many (but not all!) viable EOS.
 - Usually EOS allowing *more compact stars* ($npe\mu$ models).



Excluded:

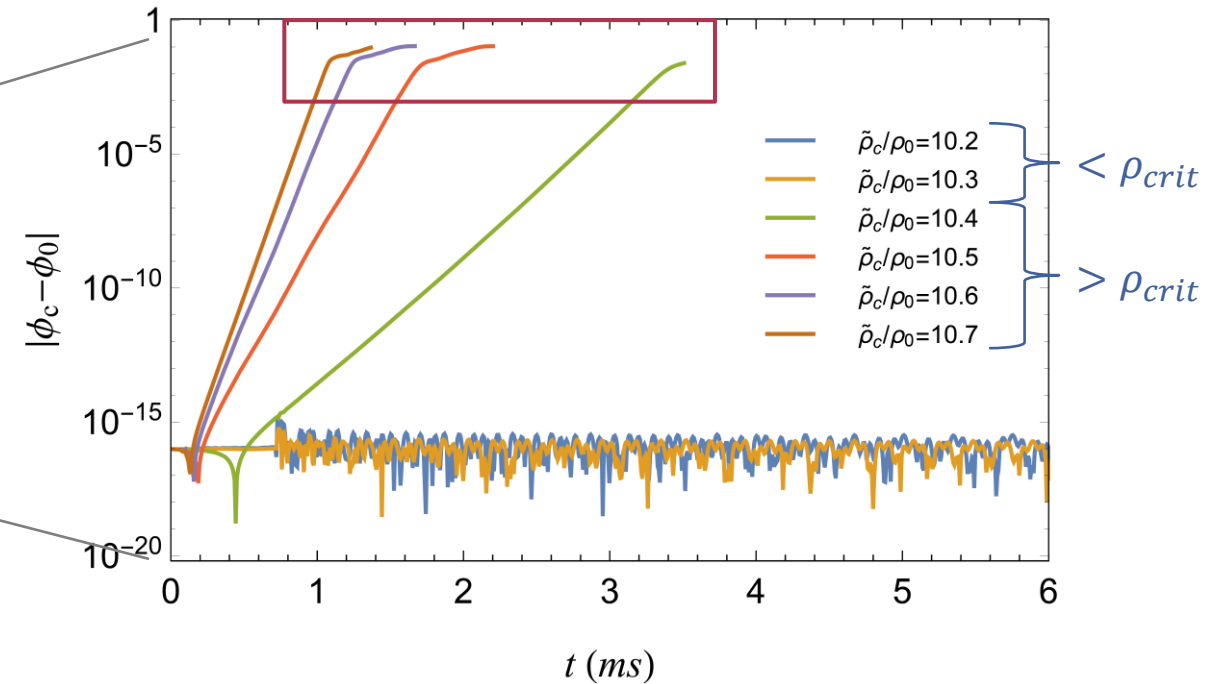
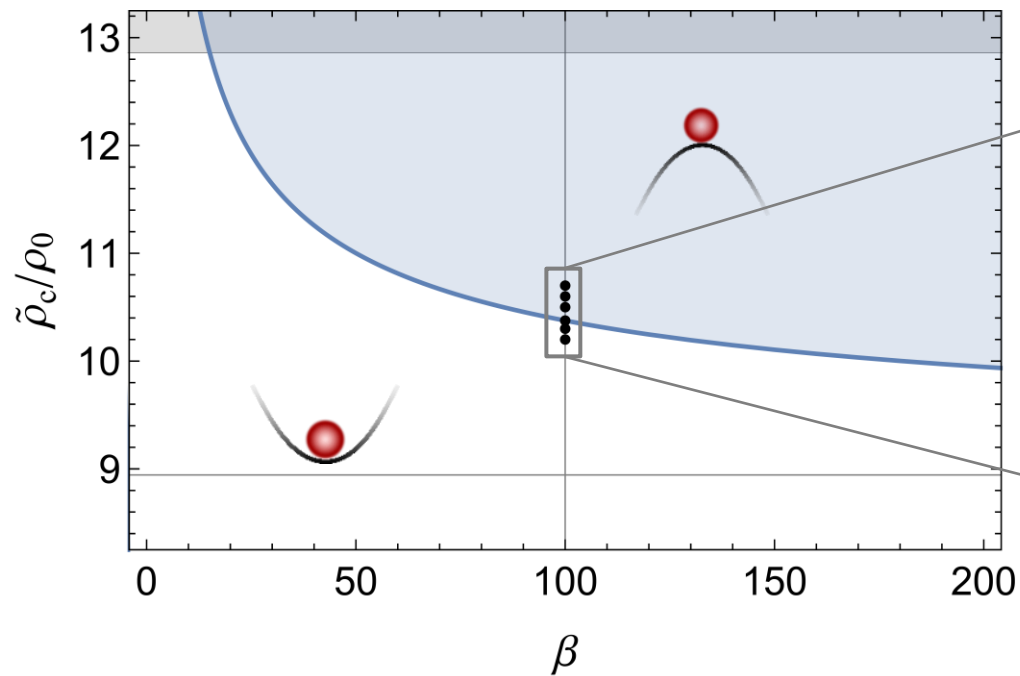
- red: $M_{\max} < 2M_{\odot}$
- blue: $c_s > 1$

Viable:

- Gray: $T < 0$
- White: $T > 0$

LINEAR STABILITY OF GR SOLUTIONS

What is the **nonlinear development** of the instability in this case?



Equil. solution
 $g_{\mu\nu} = g_{\mu\nu}^E$
 $\phi = \phi_0$

Linear scalar
 perturbation
 $\phi = \phi_0 + \delta\phi$

$$\nabla_\mu \nabla^\mu \delta\phi = -4\pi\beta T \delta\phi$$

Unstable modes if
 $m_{\text{eff}}^2 = -4\pi\beta T$
 sufficiently negative

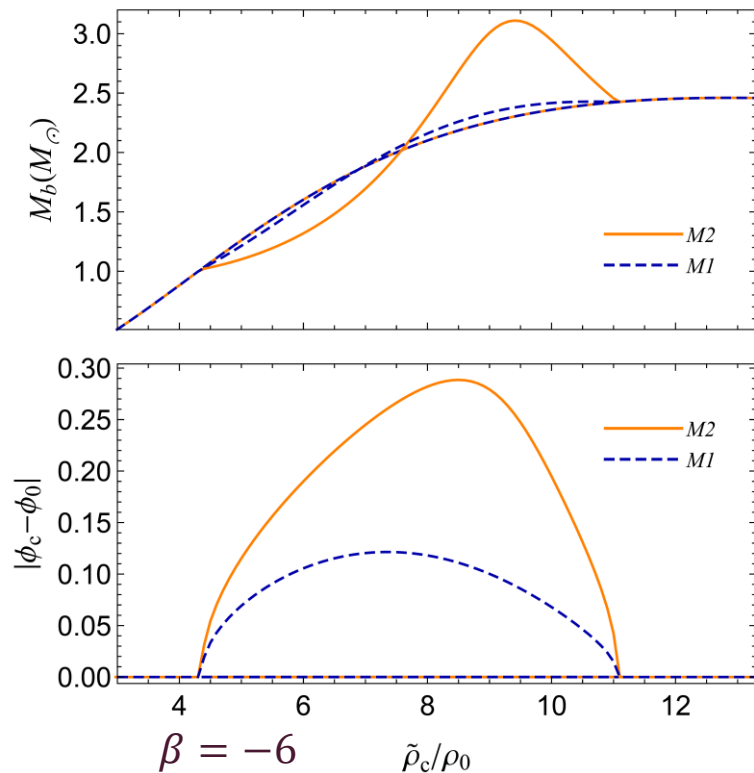
NONLINEAR DEVELOPMENT

M1: $\alpha(\phi) = \frac{1}{\sqrt{3}} \tanh[\sqrt{3} \beta (\phi - \phi_0)]$

M2: $\alpha(\phi) = \beta (\phi - \phi_0)$

$$\beta < 0$$

- GR solution unstable \Rightarrow Scalarization
 - Scalarization depends only on β
 - Details of solutions depend on $\alpha(\phi)$



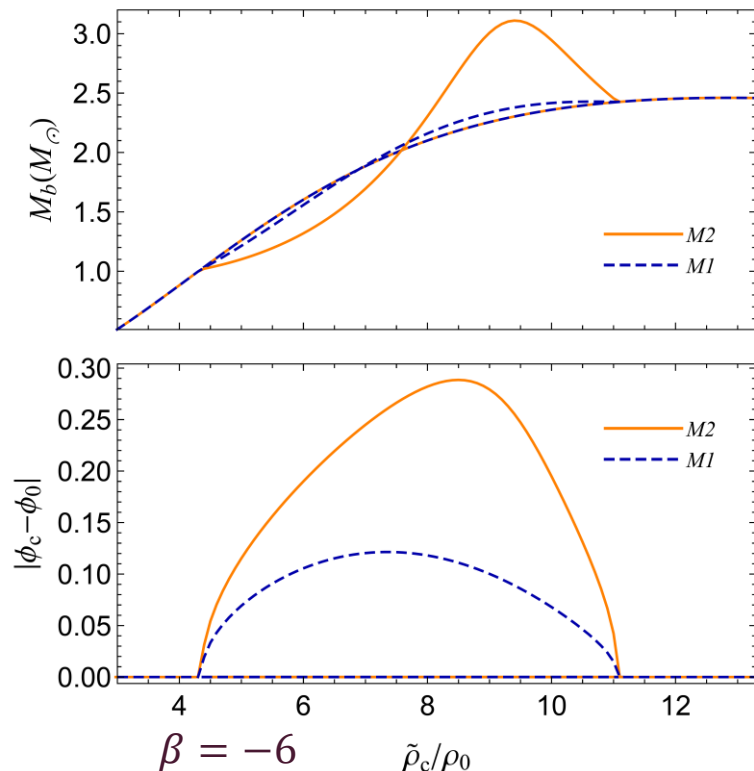
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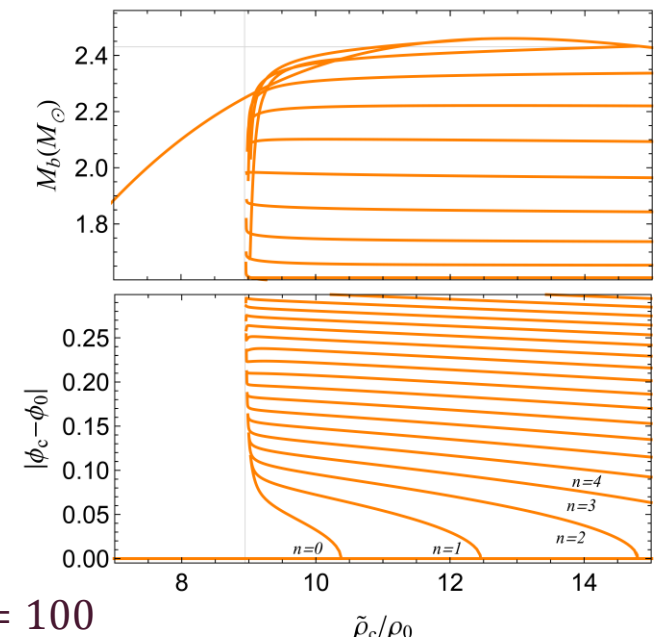
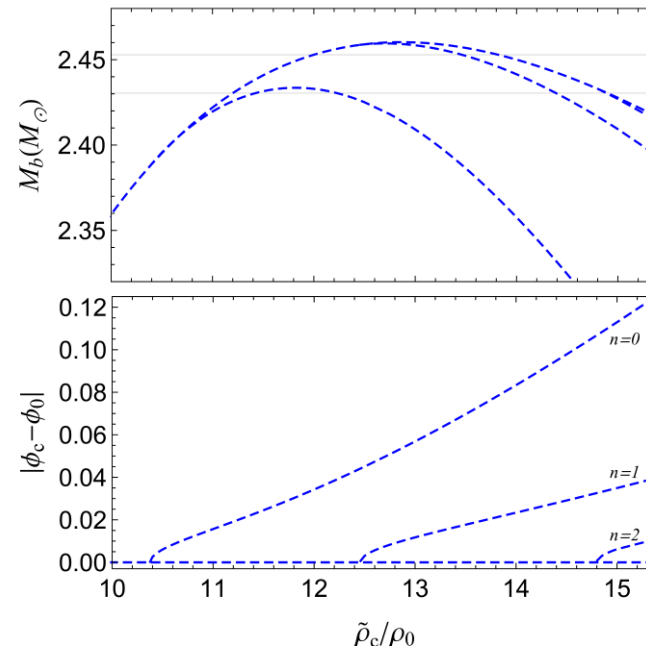
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$$\beta > 0$$

[More in N. Ortiz talk!](#)

- GR solution unstable \Rightarrow Model-dependent outcomes!
 - M1**: Spontaneous scalarization OR gravitational collapse (Mendes & Ortiz 2016)
 - M2**: gravitational collapse (Palenzuela & Liebling 2016; Mendes & Ortiz 2016)



DISCUSSION: OBSERVATIONAL CONSTRAINTS

- Current constraints on STTs with coupling function

$$\alpha(\phi) = \alpha_0 + \beta_0(\phi - \phi_0) + O[(\phi - \phi_0)^2]$$

- Solar system: $|\alpha_0| < 3.5 \times 10^{-3}$
- Pulsar timing: $\beta_0 > -4.5$
- Cosmology: potentially constrains full form of $\alpha(\phi)$. (Boisseau et al. 2000)
 - Model $\alpha(\phi) = \beta\phi$ yields bad cosmology for $\beta < 0$! (Damour & Nordtvedt 1993)
- First constraints on $\beta_0 > 0$ if NS with $M/R \gtrsim 0.27$ are confirmed.
- Observational signatures:
 - Scalarization: changes in orbital dynamics, redshift of surface atomic lines, gravitational wave emission.
 - Premature gravitational collapse: mere observation of star beyond threshold compactness!
 - Dynamical scalarization (in progress)?
- Results are sensitive to the details of the coupling function!

