

An inspiral-merger-ringdown waveform model for compact binaries on eccentric orbits

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Outline

- ❖ Motivation
- ❖ Waveform model construction
- ❖ Applications
- ❖ Future work

Motivation

- ⊛ Gravitational wave astrophysics is already revolutionizing our understanding of the Universe [GW Highlights Sessions on Tuesday]
- ⊛ Near future: accurate census of the mass and angular momentum distribution of compact sources; constraints on their channels of formation and evolution, and the environments where they reside

Extend the science reach of gravitational wave astrophysics

- ⊛ Eccentric compact binaries may form in dense stellar environments and retain eccentricity during their lifetime [*Fabian (1975), Pooley (2003), O'Leary (2009), East & Pretorius (2013), Lee et al (2010), D. Tsang (2013), L. Wen (2003), D. Tsang (2013)*]
- ⊛ Detecting these sources will provide unique insights about compact object populations in globular clusters and galactic nuclei [*MacCarone et al (2007), Irwin et al (2010), Strader et al (2012), Antonini (2014), Hopman et al (2006), Rodriguez et al (2015)*]

Motivation

- The detection of GW150914 made evident that we needed inspiral-merger-ringdown (IMR) waveform models to constrain the residual eccentricity of gravitational waves [**Ian Hinder (Monday), Adam Lewis (Thursday)**, *Arun et al 2009, Yunes et al (2009), Hinder et al 2010, Huerta and Brown (2012), Huerta et al (2014)*]
- We have developed a model that is suitable for this analysis, under the assumption that the binary components are non-spinning (Huerta, Kumar, et al. In review) [LIGO-P1600186]
- The corresponding manuscript was submitted for LIGO's internal review on June 08. It has been reviewed and accepted.

Structure of the *ax* model

PN-based
inspiral



Improved inspiral:
Self force +
Black Hole
Perturbation Theory

All known
eccentricity corrections
up to 3PN order.
Fluxes include

instantaneous, tails, tails-of-tails
contributions, and a contribution due to
non-linear memory [Arun et al (2009)]

Caveat: lacks accuracy
for systems with
asymmetric mass-ratios

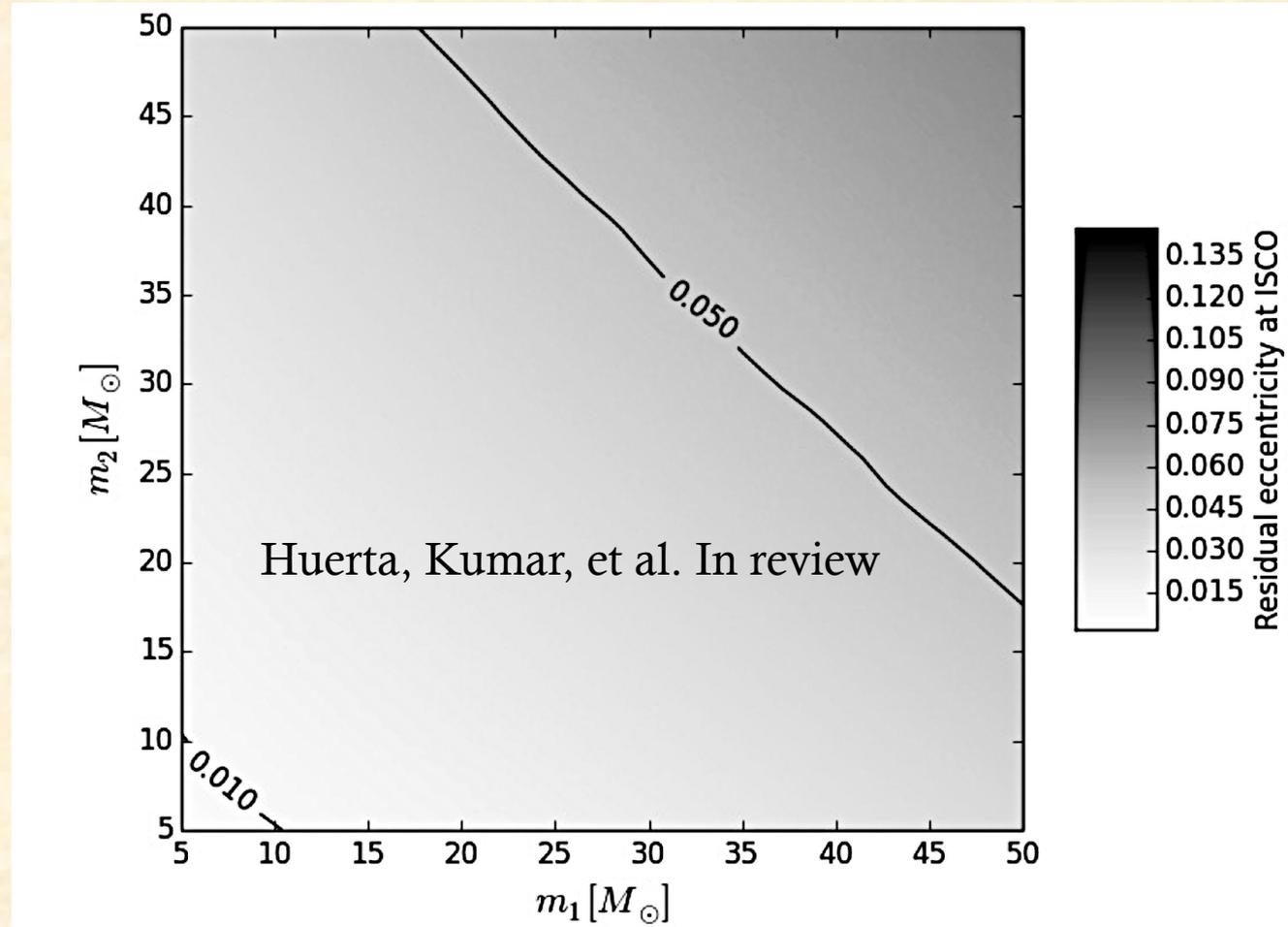
Flux of energy and binding energy
up to 6PN order including linear in
mass-ratio corrections [Fujita
(2012), Barusse et al (2012),
Damour et al (2013)]

Benefit: improves accuracy for
asymmetric
quasi-circular mass-ratio binaries

Eccentricity decay

BBH population with an initial eccentricity $e=0.3$ at a GW frequency of 15Hz.

Moderately eccentric binaries circularize prior to the merger event



Structure of the *ax* model

PN-based
inspiral



Improved inspiral:
Self force +
Black Hole
Perturbation Theory



Quasi-circular
merger waveform

All known corrections
up to 3PN order.

Fluxes include
instantaneous terms, tails,
tails-of-tails contributions
and non-linear memory

Caveat: lacks accuracy
for systems with
asymmetric mass-ratios

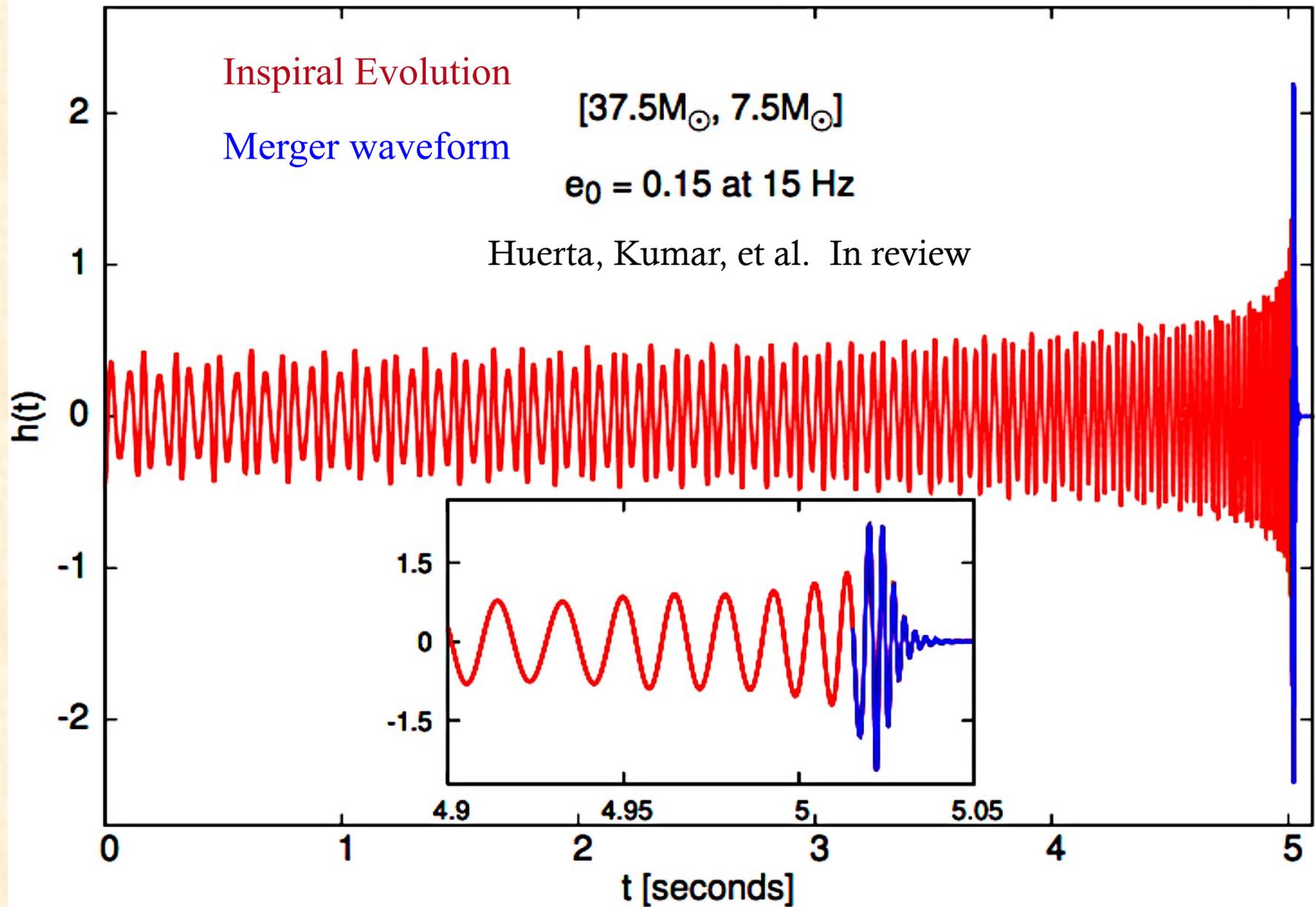
Flux of energy and
binding energy up to
6PN order including
linear in mass-ratio
corrections

Benefit: improves
accuracy for
asymmetric
mass-ratio binaries

Implicit Rotating
Source (IRS) formalism
calibrated with numerical
relativity simulations up to
mass-ratio 10 [Baker et al
(2008), Kelly et al (2010)]

Caveat: very accurate only
in the vicinity of the light-
ring

Complete waveform

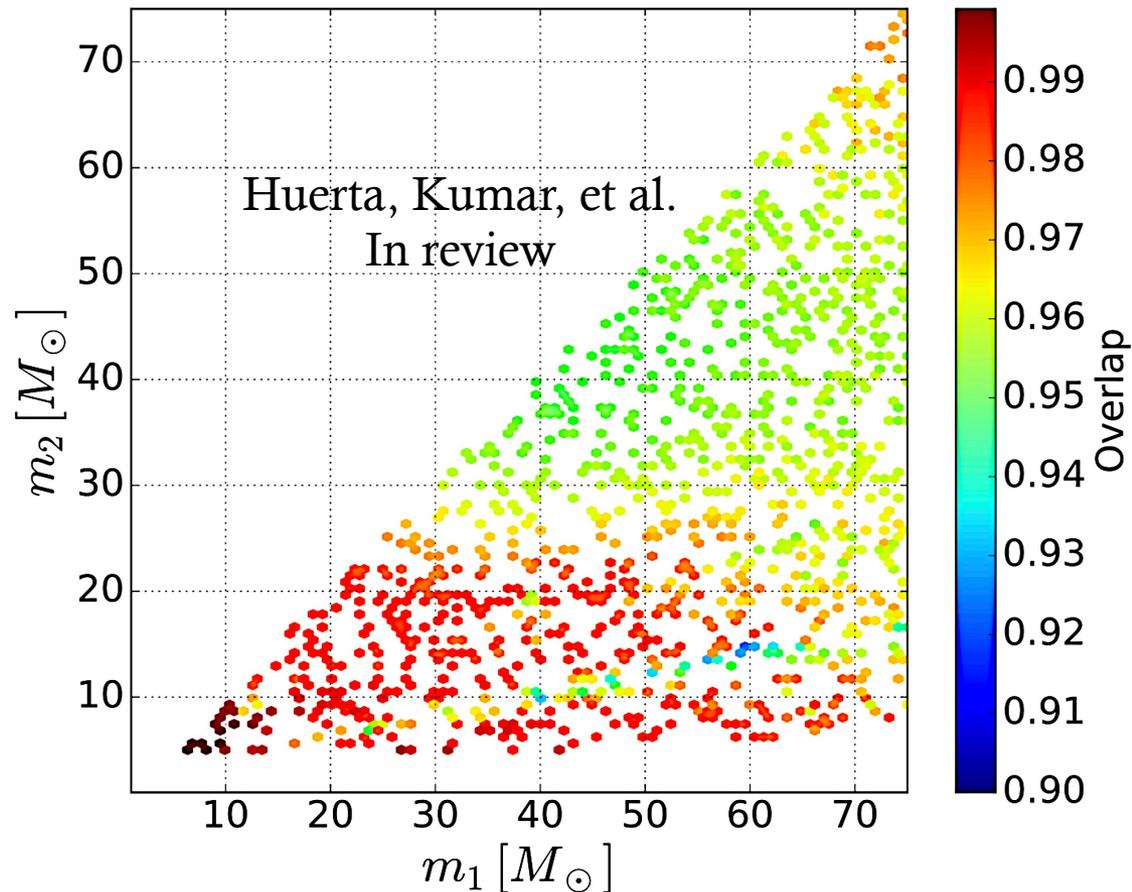


Comparison to state-of-the-art quasi-circular waveforms in the zero eccentricity limit

PSD: mid-aLIGO

Initial filtering frequency: 25Hz

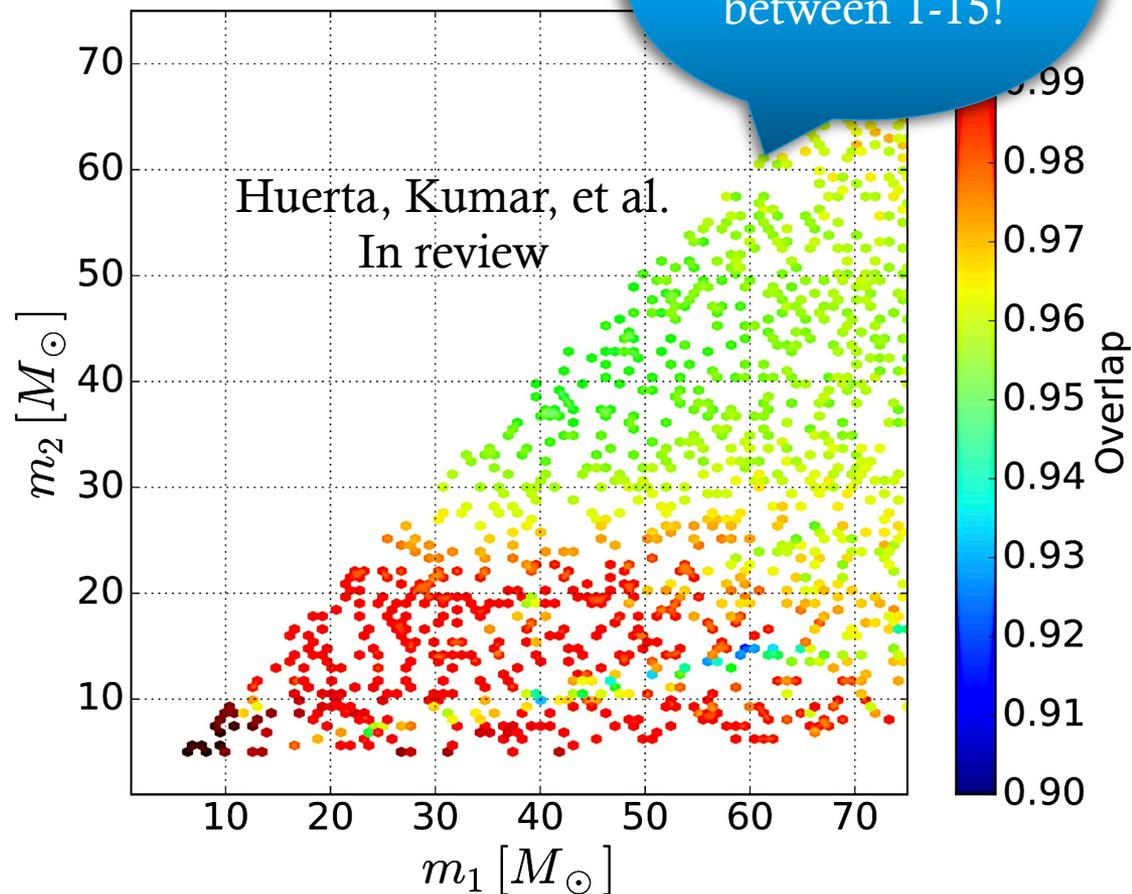
IMR eccentric model agrees
well with the effective-one-
body model (EOBNRv2) over a
wide range of the BBH
parameter space accessible to
aLIGO



Comparison to EOBNRv2 in the zero eccentricity limit

PSD: mid-aLIGO
Initial filtering frequency:
25Hz

IMR eccentric model agrees
well with EOBNRv2 over a
wide range of the BBH
parameter space accessible to
aLIGO



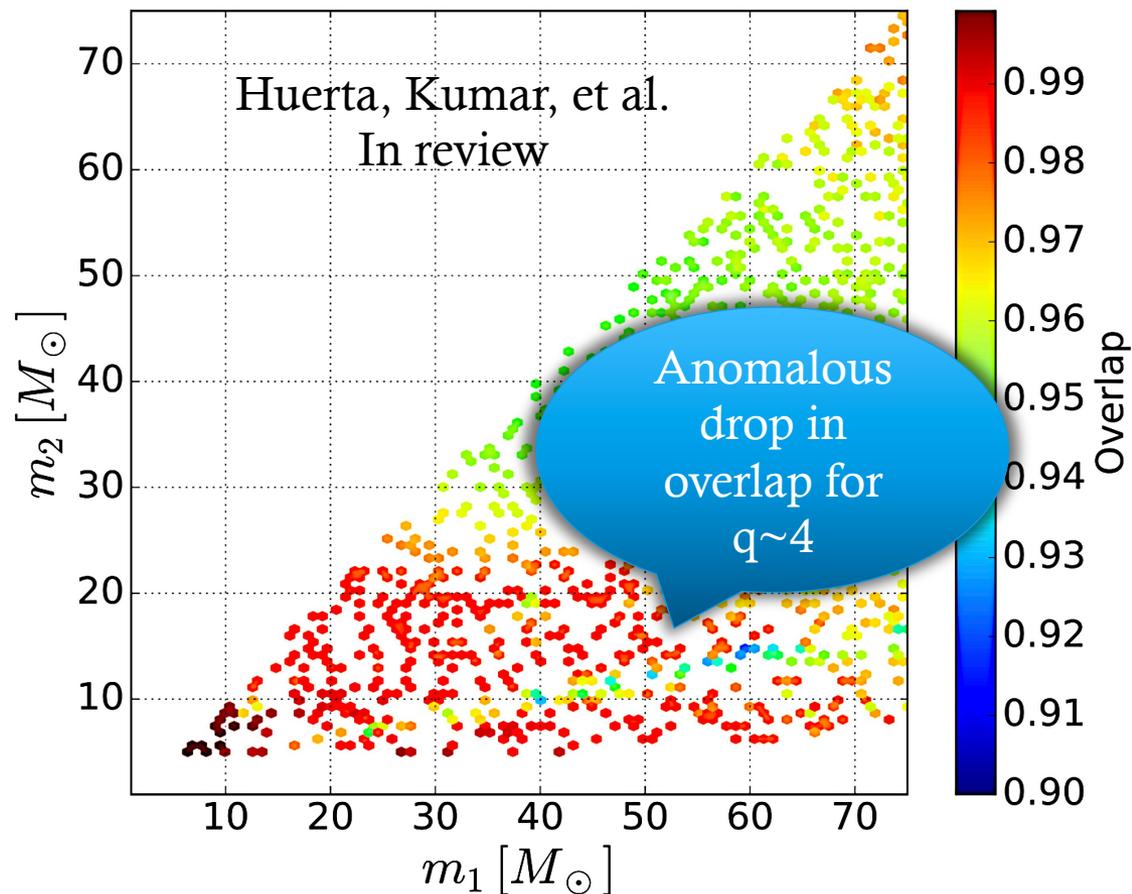
Comparison to EOBNRv2 in the zero eccentricity limit

PSD: mid-aLIGO

Initial filtering frequency:
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IMR eccentric model agrees
well with EOBNRv2 over a
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Improved version of the
merger waveform using a
larger set of NR simulations

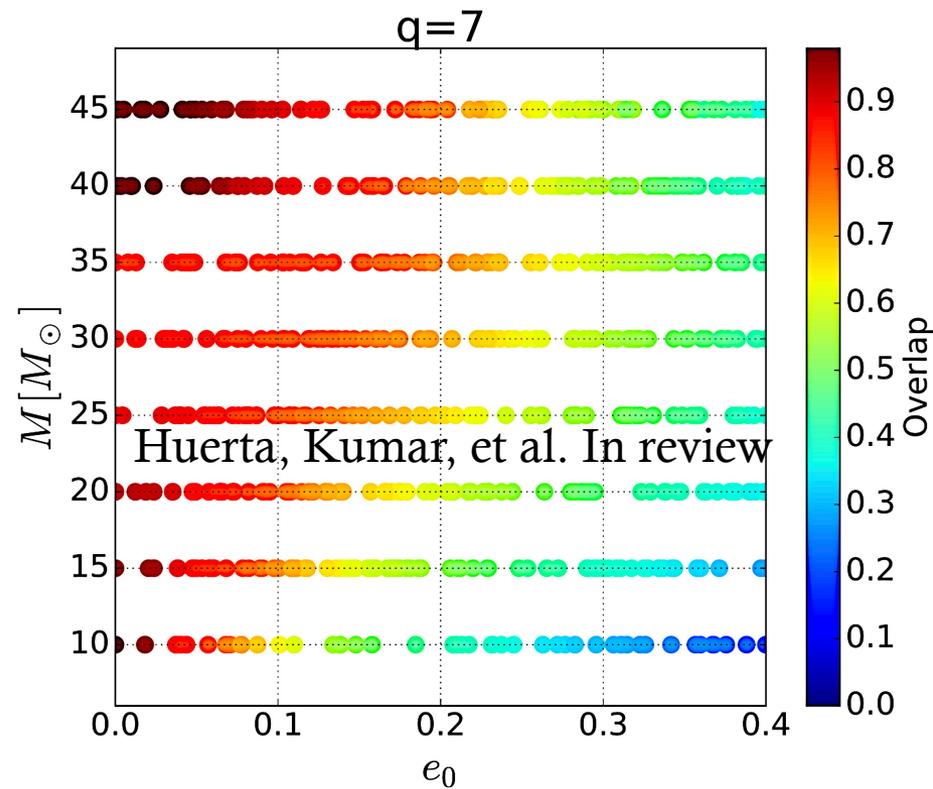
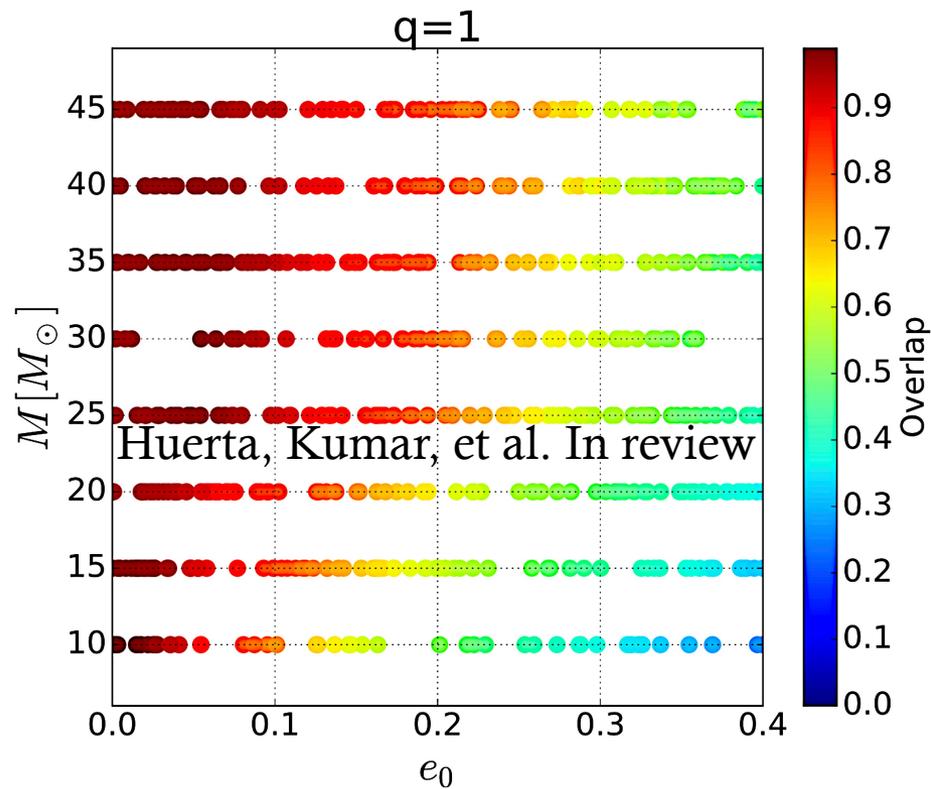


Applications

PSD: Zero Detuned High Power

Initial filtering frequency: 15Hz

Eccentricity of x-axis defined at a GW frequency of 15Hz



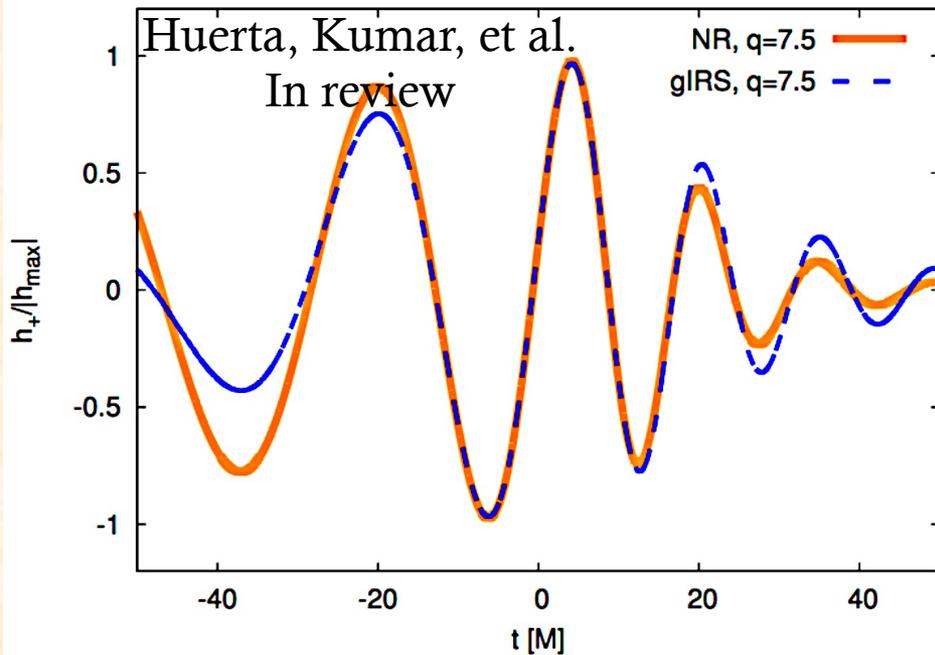
Improving the merger model

NCSA: Miguel Holgado and Erik Wessel

Cambridge: Alvin Chua and Chris Moore

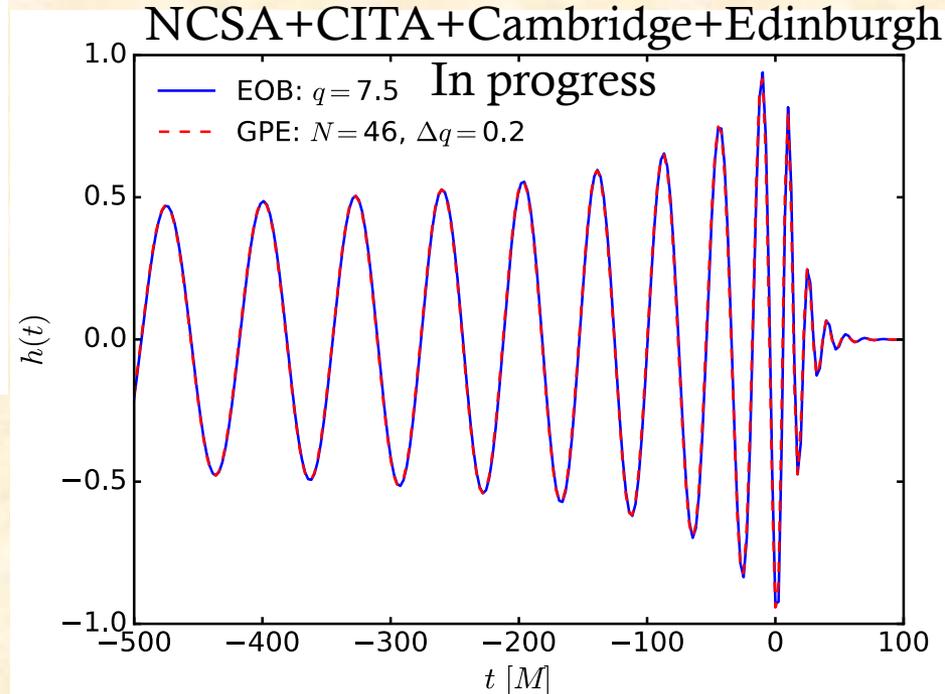
CITA: Harald Pfeiffer and Prayush Kumar

Edinburgh: Jon Gair



gIRS works very well *in the vicinity of the light-ring*

Our new approach works very well *several cycles before merger!*



Future work

- ⊗ With Ian Hinder: quantify the accuracy of our IMR models using numerical relativity simulations for astrophysically motivated sources
- ⊗ We will use our models to quantify how accurately we can constrain the residual eccentricity of new detections with aLIGO
- ⊗ We are developing new tools to detect and characterize eccentric sources. Network of collaborators: NCSA (USA), CITA (Canada), Cambridge (UK), Edinburgh (UK), AEI (Germany) and ICTS (India)

Conclusions

- ⊗ We have combined PN, self-force, black hole perturbation theory and numerical relativity to develop the first IMR model that can describe eccentric binaries with asymmetric mass-ratios
- ⊗ We have shown that the model agrees well with EOBNRv2 in the zero eccentricity limit
- ⊗ An improved version of the model is currently under construction to address two key issues:
 - ⊗ Increase overlap with EOBNRv2 in the quasi-circular limit
 - ⊗ Include spin of the binary components

Inspiral dominated systems

Power Spectral Density: Zero Detuned High Power

Initial frequency for filtering: 15Hz

Eccentricity on the x-axis defined at a GW frequency of 15Hz

TaylorT4 3.5PN vs *ax* model

